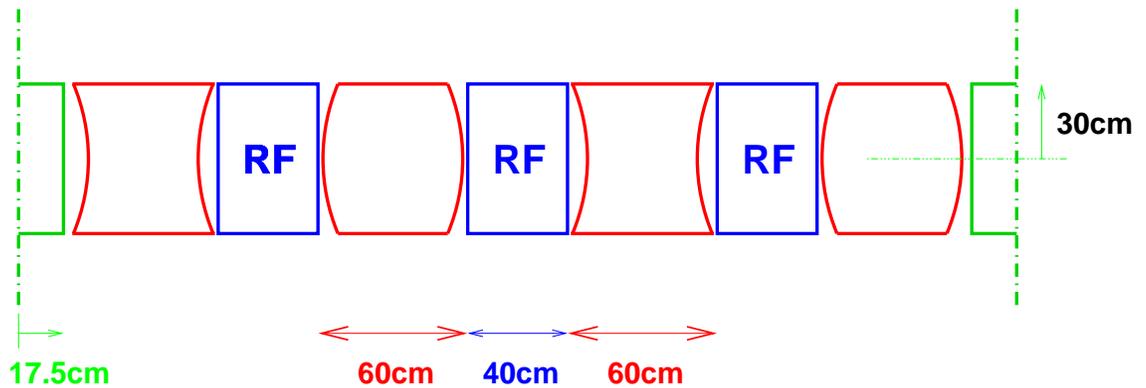


# Fringe Field Effects in Quadrupole Cooling Channels

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E-exchange meeting, Fermilab, 6/11/2002

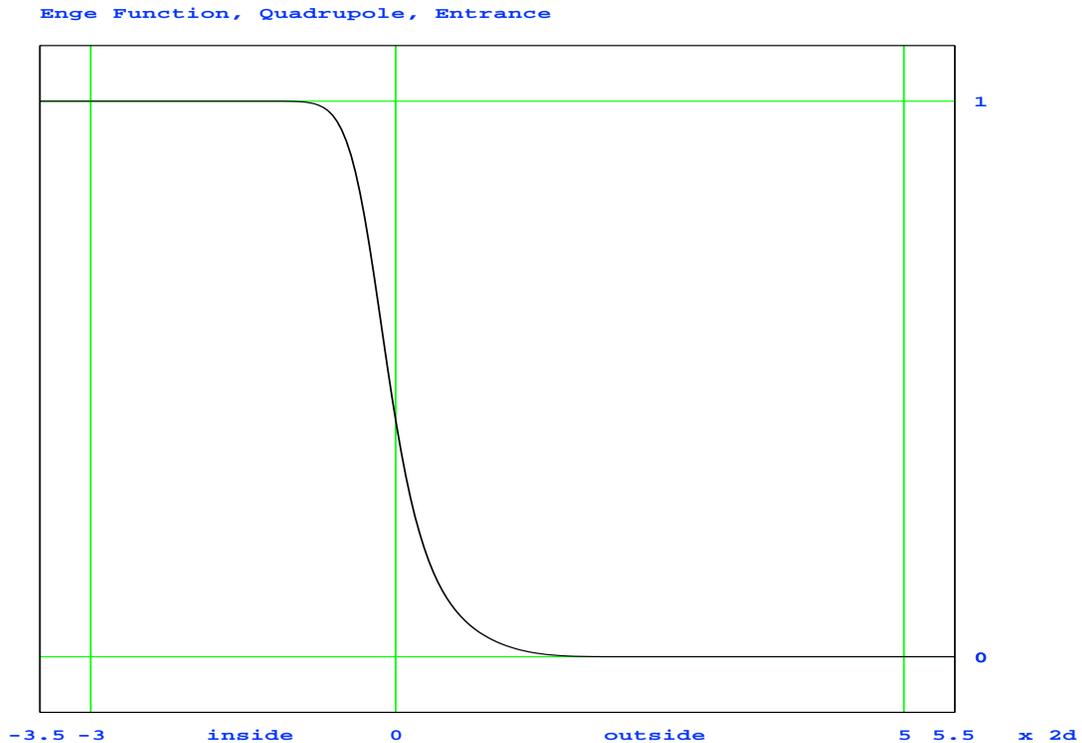
# Enge Function for the Fringe Field Fall-off

$$F(s) = \frac{1}{1 + \exp(a_1 + a_2 \cdot (s/D) + \dots + a_6 \cdot (s/D)^5)}$$

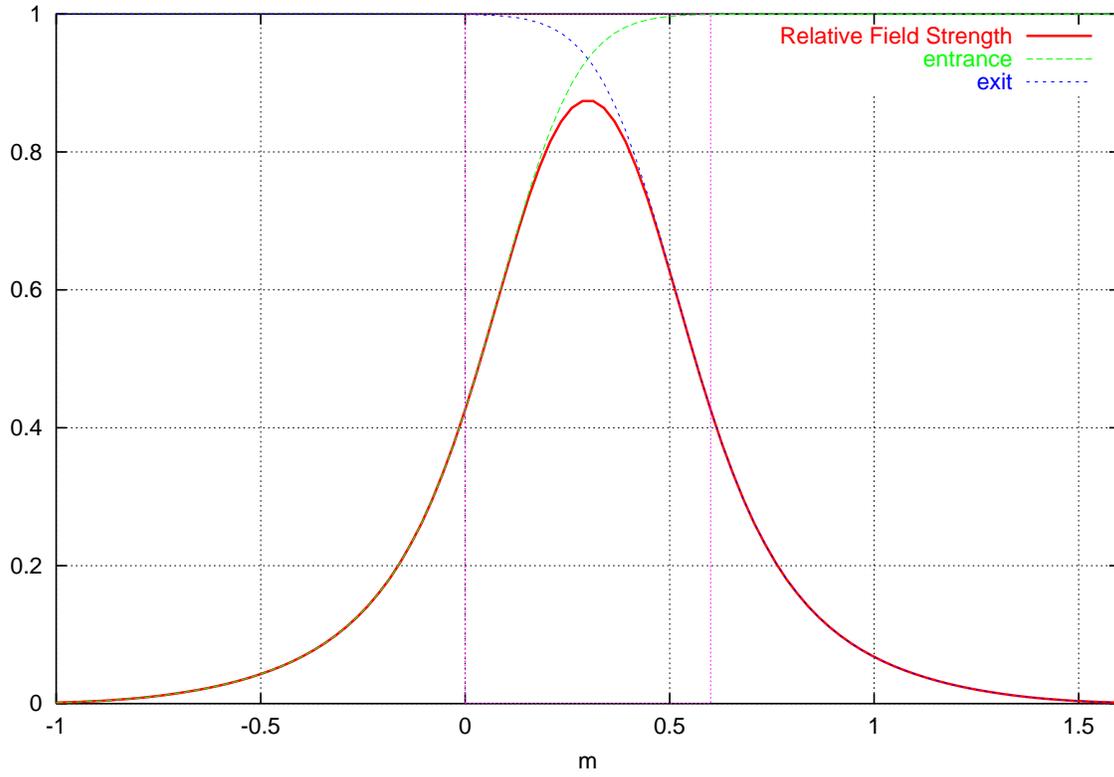
$D$  : the full aperture

## Enge Coefficients of Various Quadrupoles

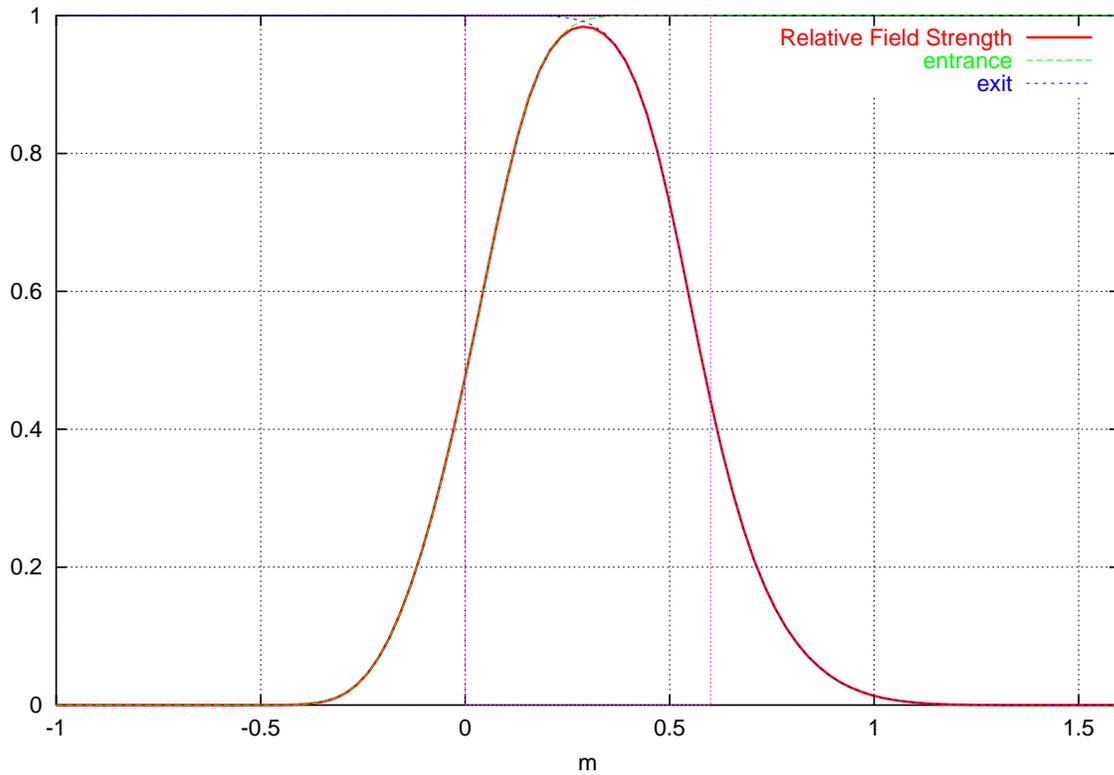
		$a_1$	$a_2$	$a_3$	$a_4$	$a_5$	$a_6$
SLAC-PEP		0.296471	4.533219	-2.270982	1.068627	-0.036391	0.022261
S800 Q II	Entr.	0.0965371	6.63297	-2.718	10.9447	1.64033	0.00
	Exit	0.235452	6.60424	-3.42864	4.38392	-0.573524	0.00
LHC-HGQ lead		-0.939436	3.824163	3.882214	1.776737	0.296383	0.013670



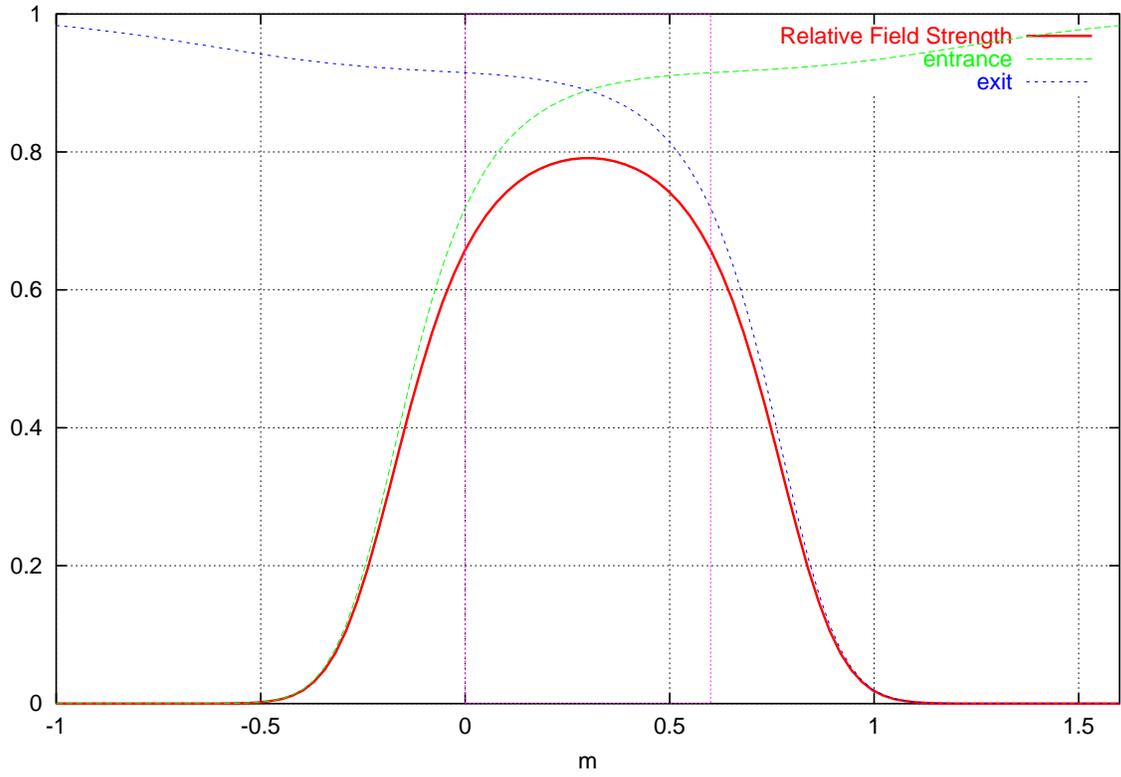
MQ Enge fall-off (measurement from PEP/SLAC) for 60cm full aperture, 60cm length



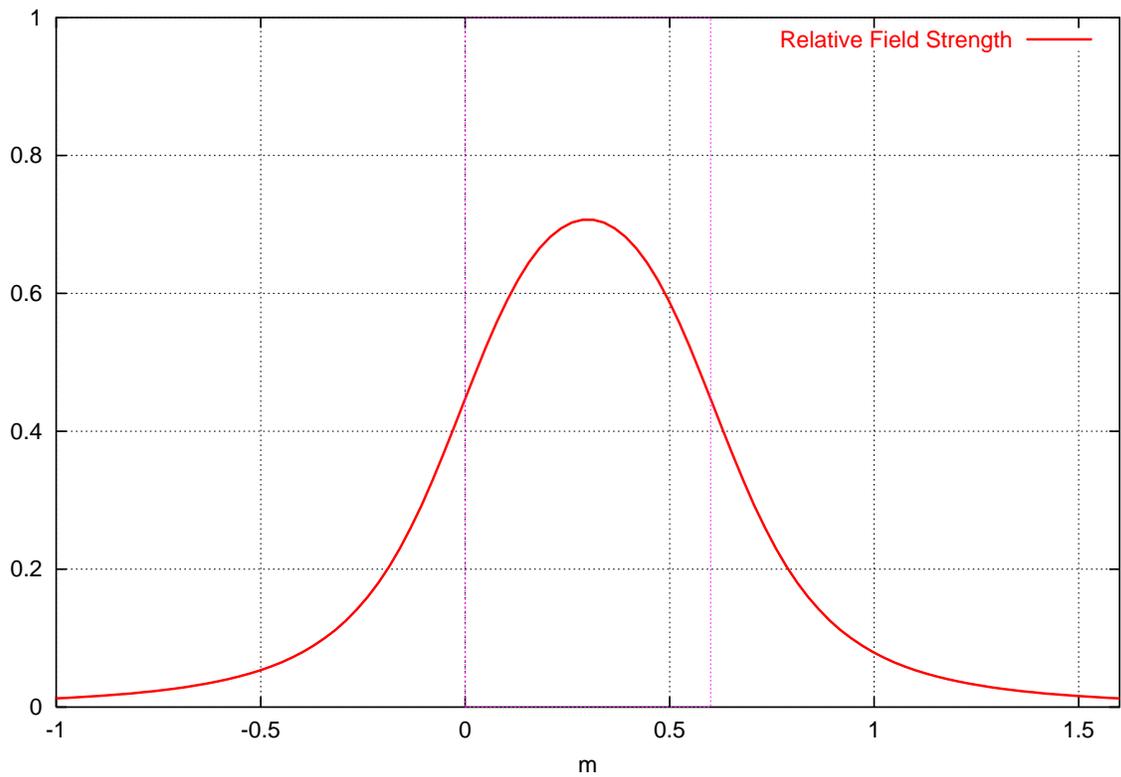
MQ Enge fall-off (measurement from MSU/S800 Quad II) for 60cm full aperture, 60cm length



MQ Enge fall-off (measurement from LHC/HGQ lead end) for 60cm full aperture, 60cm length



Ideal Solenoid for 60cm full aperture, 60cm length



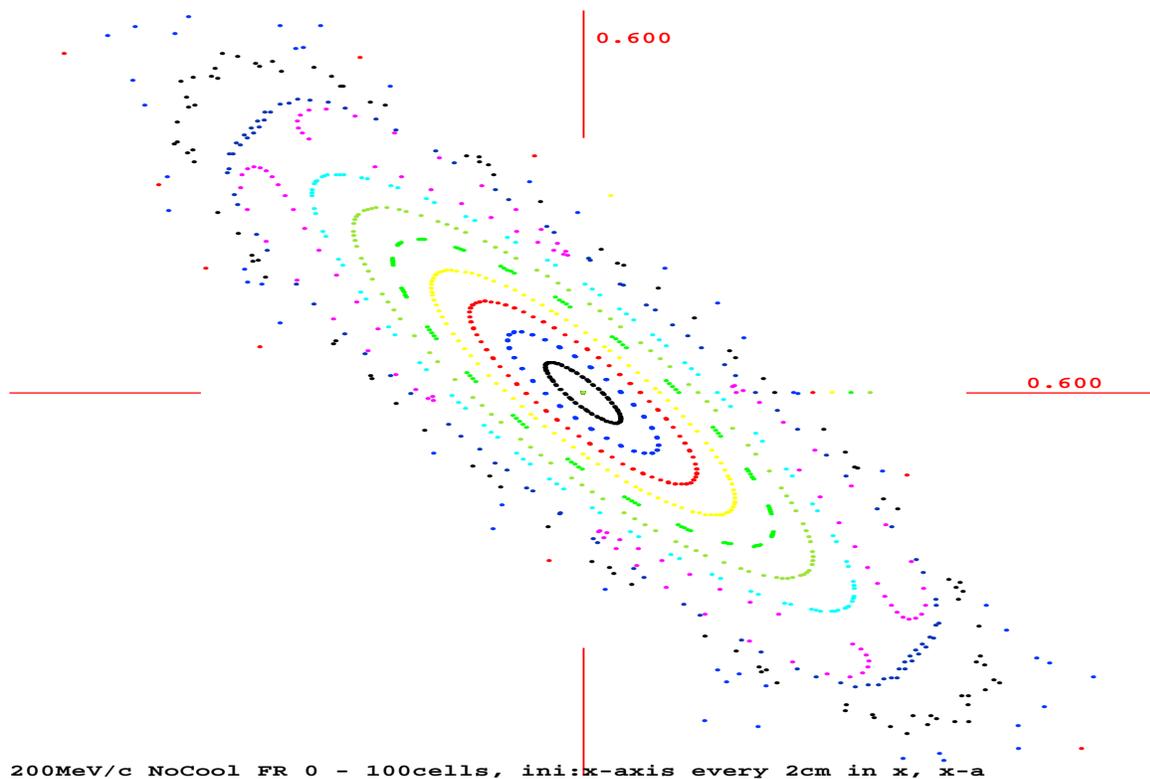
# Fringe Field Effects on Quad Channel Tracking

200 MeV/c Particles along the  $x$ -axis at every 2cm are tracked through 100 Quad cells (without cooling, nor acceleration).

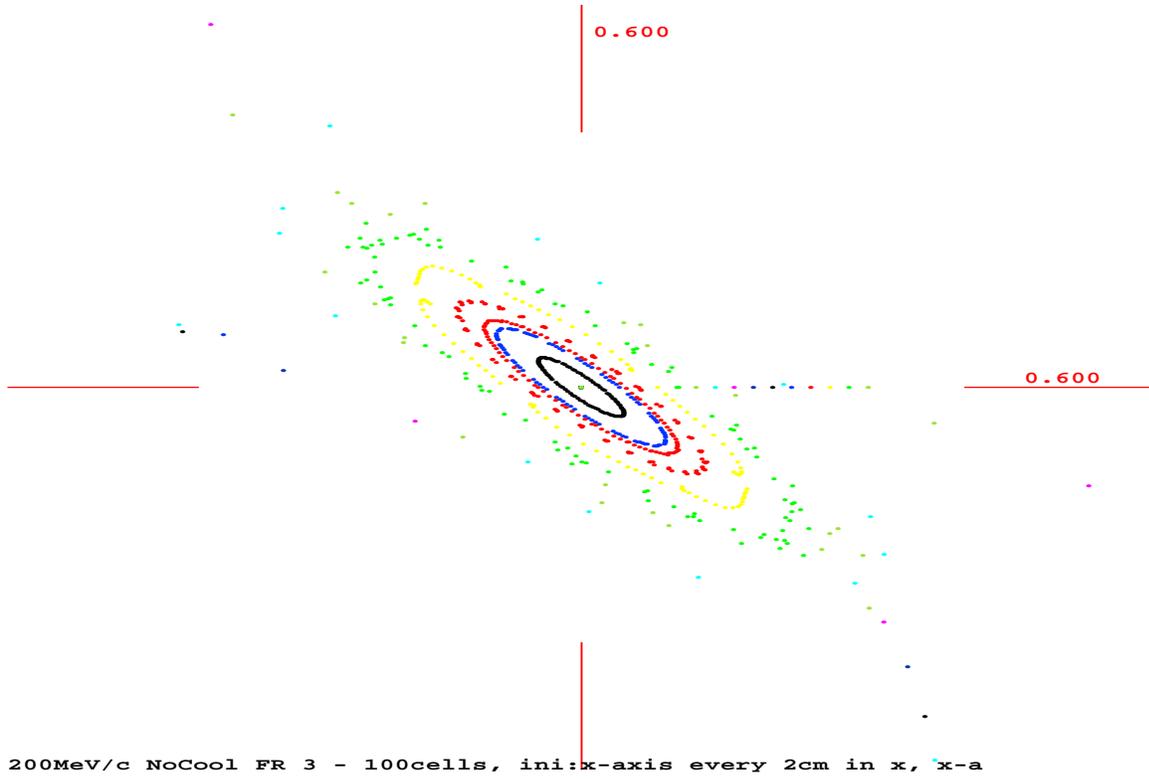
The pictures are shown in the  $x - p_x/p_0$  plane in the frame size 60cm  $\times$  0.6 rad.

(The title page shows the cell for this study.)

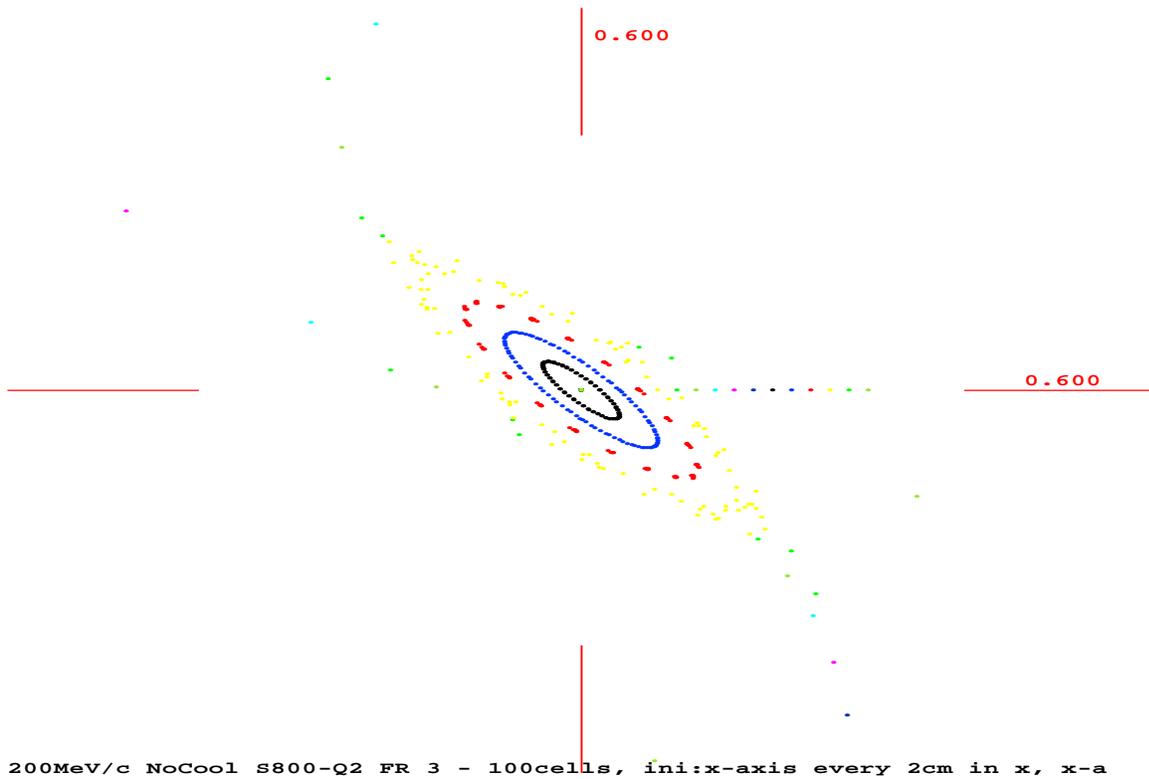
## Sharp Cut-off Fringe Field Model ( No Fringe Field Effect Consideration )



# PEP/SLAC Quad Fringe Field Fall-off Model



# S800 Q II Quad Fringe Field Fall-off Model



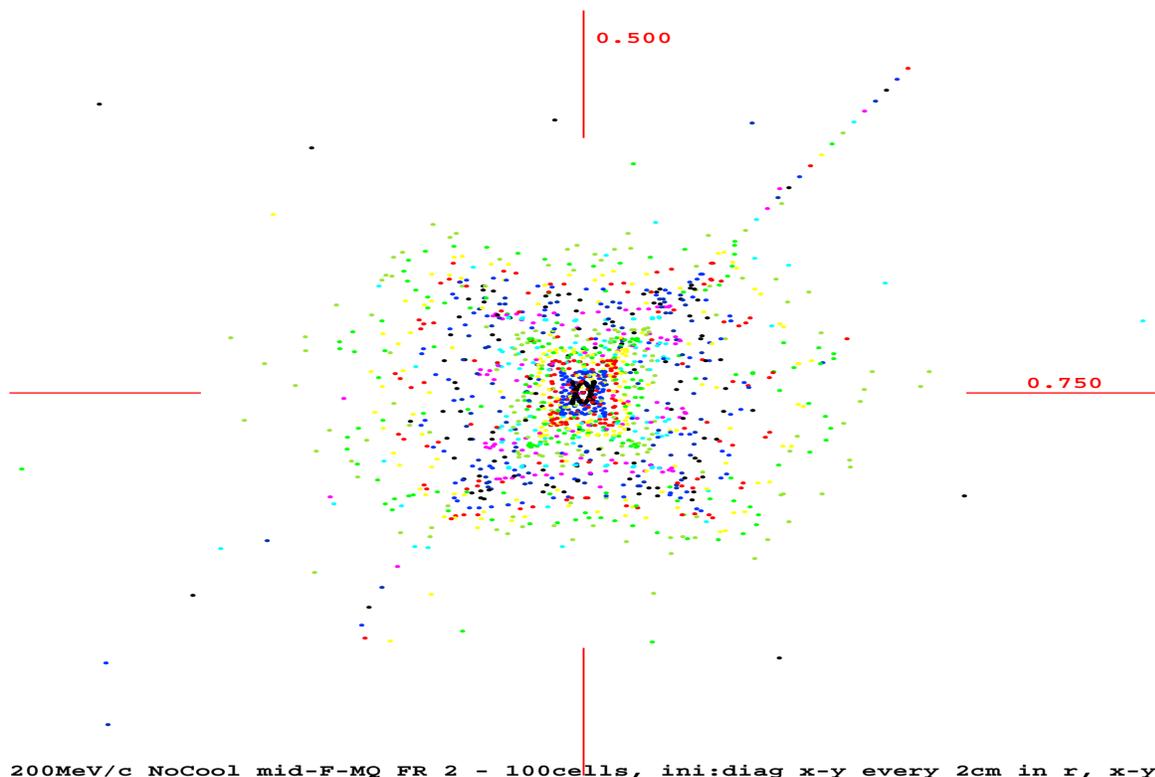
# Off Particles' Survival through the Channel

200 MeV/c Particles are tracked through 100 cells, where each cell starts in **the middle of focusing** quad ( $\beta_x$  is maximum). Particles start at every 2cm along

- (1) the  $x$  axis,
- (2) the  $y$  axis,
- (3) the  $x$ - $y$  diagonal.

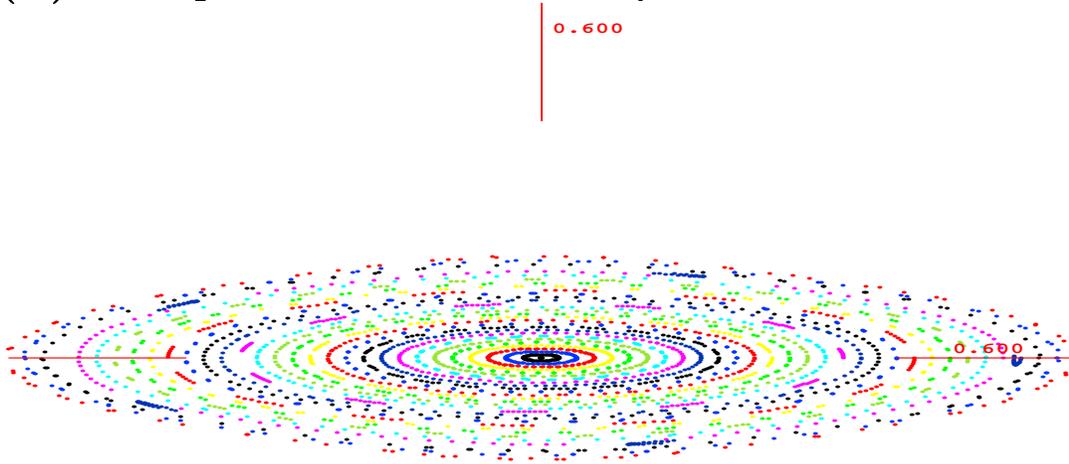
COSY's fast fringe field computation mode (FR 2) is used with model for SLAC/PEP.

- (3) in the  $x - y$  plane with frame size 75cm  $\times$  50cm.  
The  $x$  direction survives more.



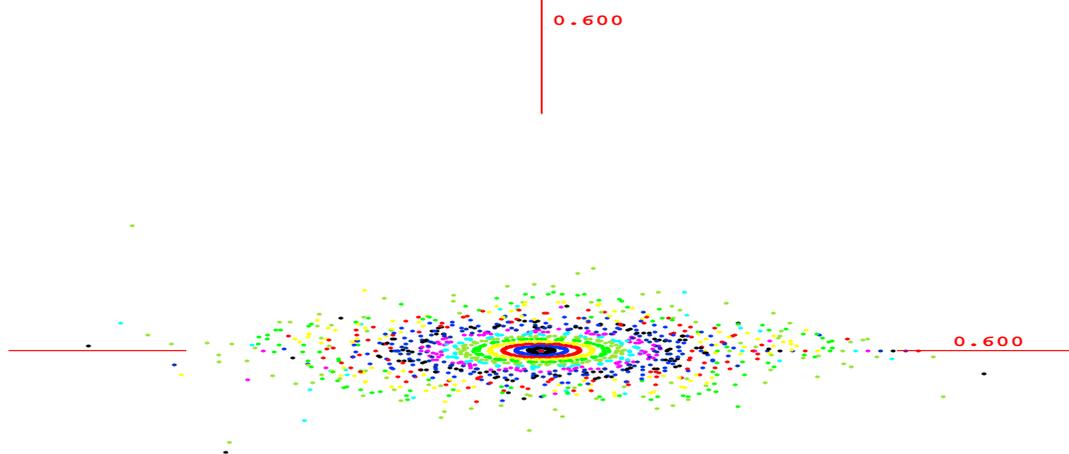
In the  $x - p_x/p_0$  plane with frame size 60cm  $\times$  0.6 rad.

(1) The particles survive fully.



200MeV/c NoCool mid-F-MQ FR 2 - 100cells, ini:x-axis every 2cm in r, x-a

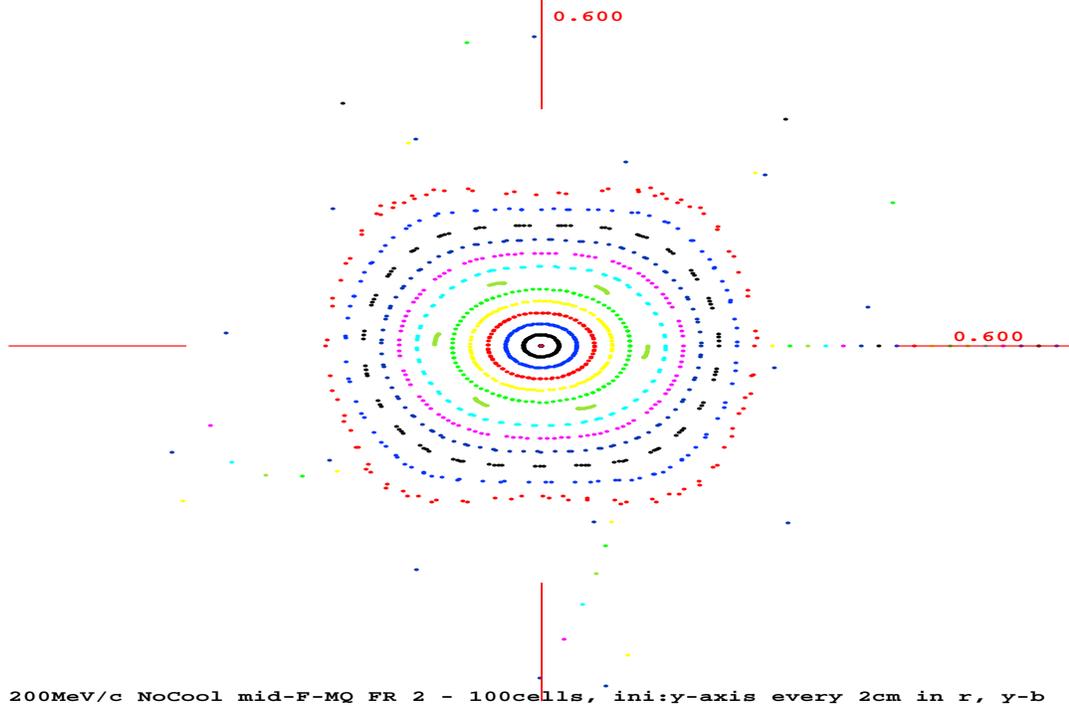
(3) Projected from the picture in page 7.



200MeV/c NoCool mid-F-MQ FR 2 - 100cells, ini:diag x-y every 2cm in r, x-a

In the  $y - p_y/p_0$  plane with frame size 60cm  $\times$  0.6 rad.

(2) The particles starting from the low  $\beta$  survive.



(3) Projected from the picture in page 7.

