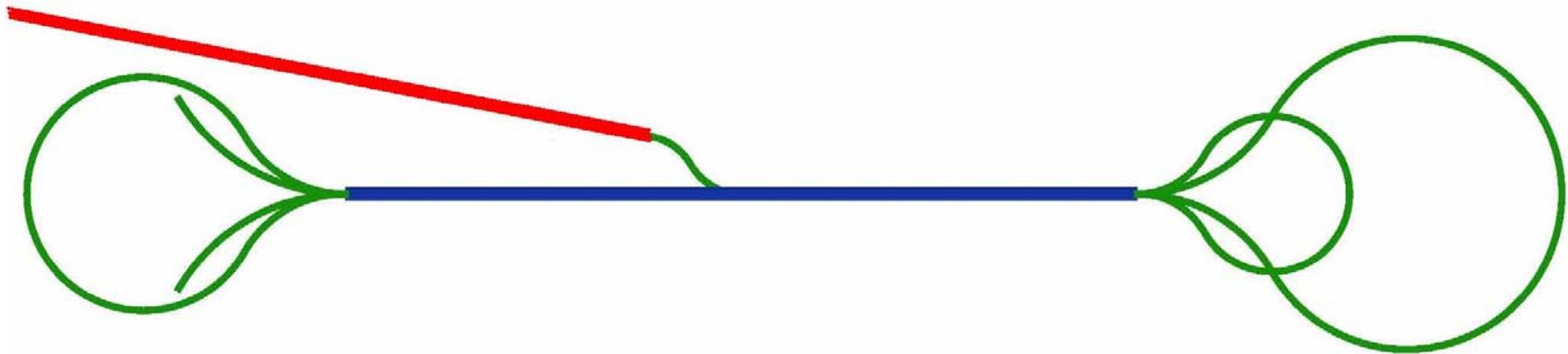


Low Energy Stages - 'Dogbone' Muon RLA

Alex Bogacz

- Ⓢ FFAG acceleration below 5GeV not feasible (cost effective)
- Ⓢ 'Dogbone' RLA (3.5-pass) scheme based on 200MHz SRF
 - Pre-accelerator (273 MeV/c – 1.5 GeV) based on solenoid focusing
 - Main Linac (1 GeV/pass) based on triplet focusing
 - Three Arcs with horizontal multi-pass separation
- Ⓢ Initial beam parameters for Study IIa – after cooling at 273 MeV/c
- Ⓢ Lattices – linear optics, tracking studies

'Dogbone' RLA (3.5-pass) scheme



- Pre-accelerator (273 MeV/c – 1.5 GeV) – solenoid focusing
- Main Linac (1 GeV/pass) – triplet focusing
- Single magnet horizontal multi-pass separation
- 3 Arcs based on the same strength of bending magnets (~ 1 Tesla)

Initial beam emittance/acceptance after cooling at 273 MeV/c

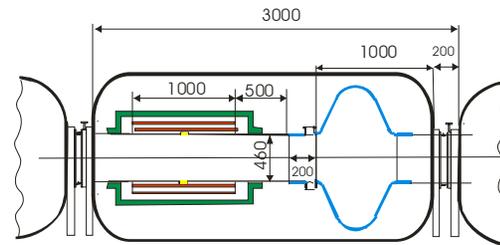
Study IIa		ϵ_{rms}	$A = (2.5)^2 \epsilon$
normalized emittance: ϵ_x/ϵ_y	mm·rad	4.8	30
longitudinal emittance: ϵ_l ($\epsilon_l = \sigma_{\Delta p} \sigma_z / m_\mu c$)	mm	27	150
momentum spread: $\sigma_{\Delta p/p}$		0.07	±0.17
bunch length: σ_z	mm	176	±442

Machine Parameters

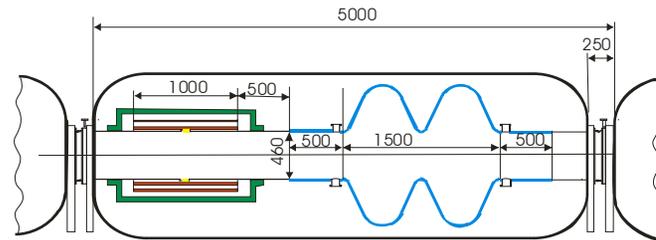
Study IIa		
Final energy	GeV	5
Number of bunches per pulse		89
Number of particles per pulse		$3 \cdot 10^{12}$
Bunch/accelerating frequency	MHz	200/200
Average repetition rate	Hz	15
Average beam power	kW	144

Pre-accelerator – 3 styles of cryo-modules, solenoid focusing

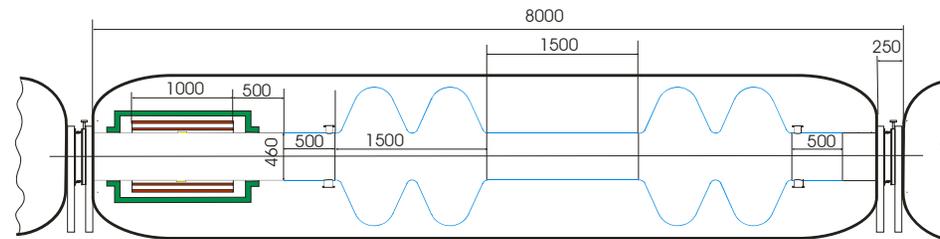
◆ short (3 m)



◆ medium (5 m)



◆ long (8 m)



Blue – SC walls of cavities. Red – solenoid coils. Green – magnetic shielding.

❖ Pre-accelerator – parameters of different style cryo-modules

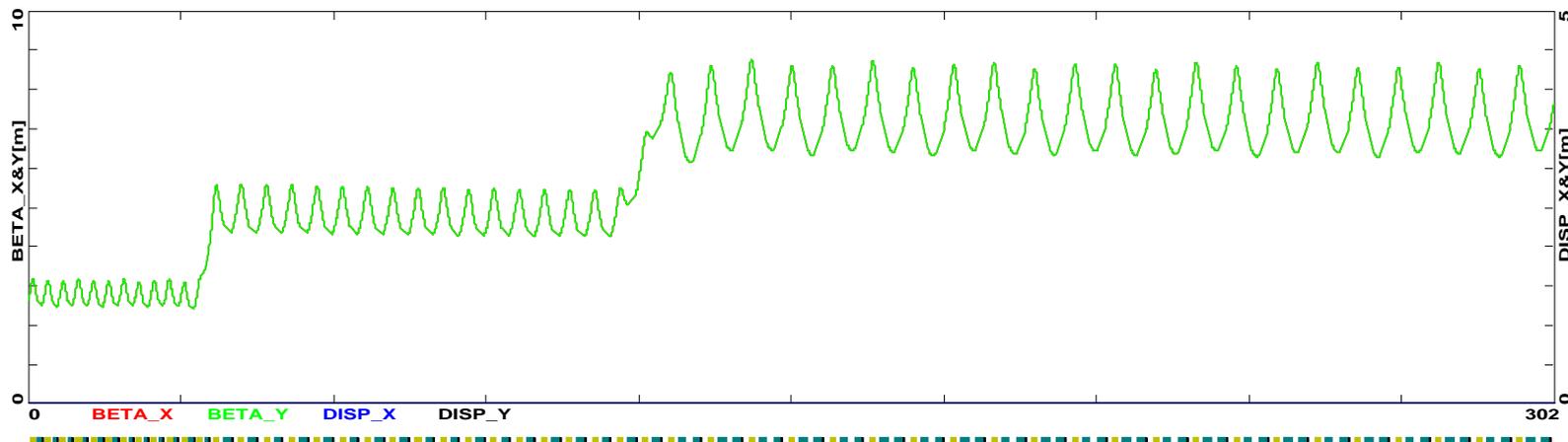
	Short	Medium	Long
Number of periods	12	18	22
Total length of one period	3 m	5 m	8 m
Number of cavities per period	1	1	2
Number of cells per cavity	1	2	2
Cavity accelerating gradient	15 MV/m	15 MV/m	15 MV/m
Real-estate gradient	3.72 MV/m	4.47 MV/m	5.59 MV/m
Aperture in cavities (2a)	460 mm	460 mm	460 mm
Aperture in solenoids (2a)	460 mm	460 mm	460 mm
Solenoid length	1 m	1 m	1 m
Solenoid maximum field	1.5 T	1.9 T	3.9 T

Total length: **302 m**

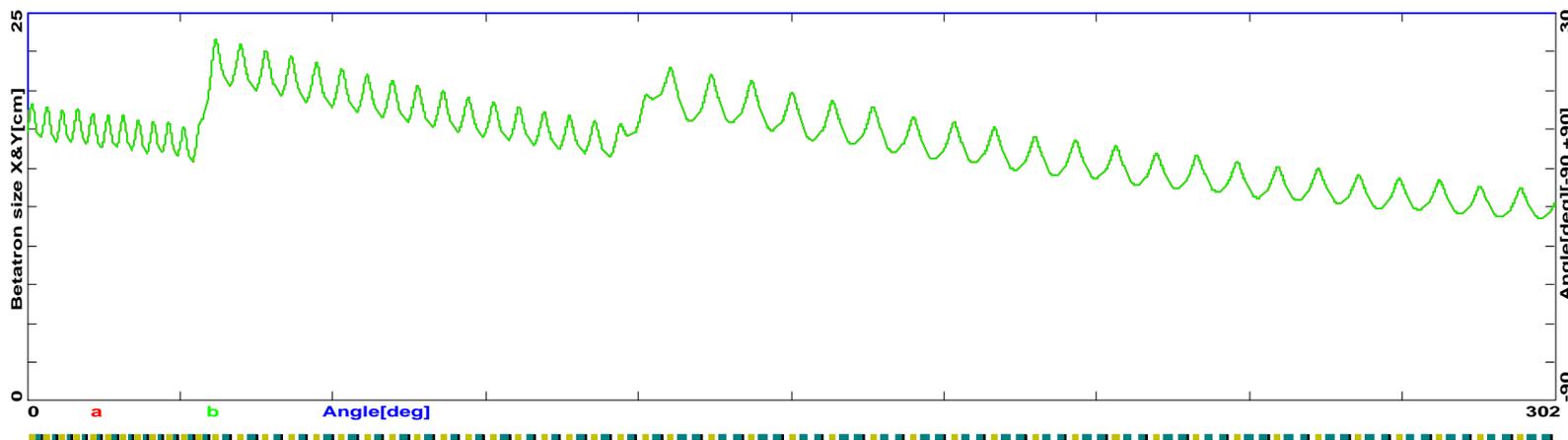
Total gradient: **2.07 GV**

◆ Linear Pre-accelerator – Twiss functions and beam envelope (2.5σ)

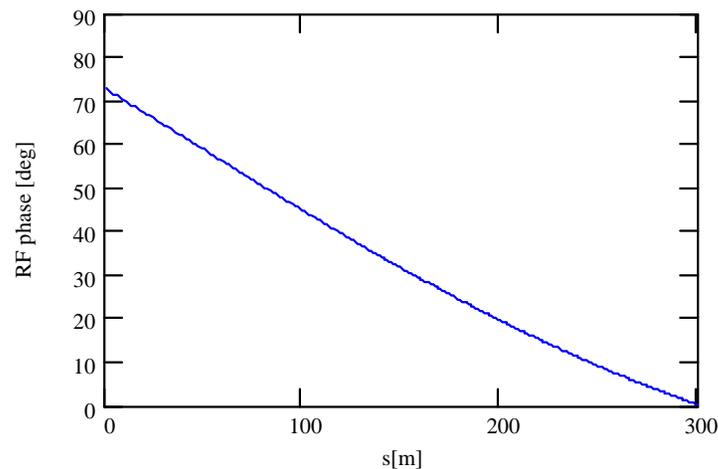
Fri Dec 03 09:03:52 2004 OptiM - MAIN: - D:\Study 2A\PreLinac\Linac_sol.opt



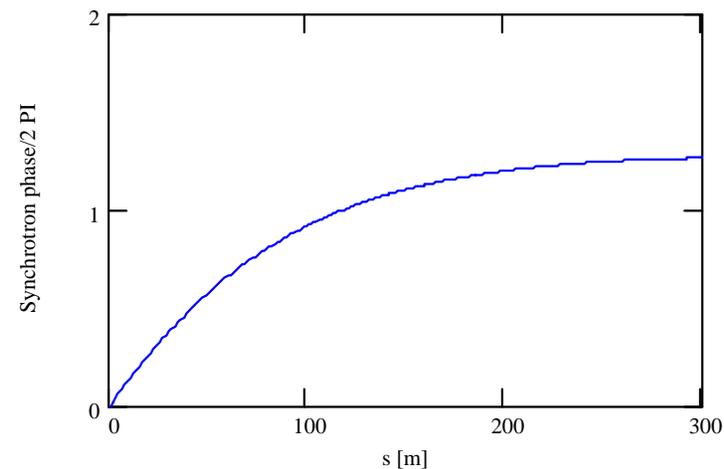
Fri Dec 03 11:22:15 2004 OptiM - MAIN: - D:\Study 2A\PreLinac\Linac_sol.opt



- ❖ Introduction of synchrotron motion in the initial part of the linac
 - ◆ allows to perform adiabatic bunching/compression of the beam
 - ◆ prevents head-to-tail 'sag' in acceleration
 - ◆ reduction of effective accelerating gradient (1.3GV out of 2 GV)

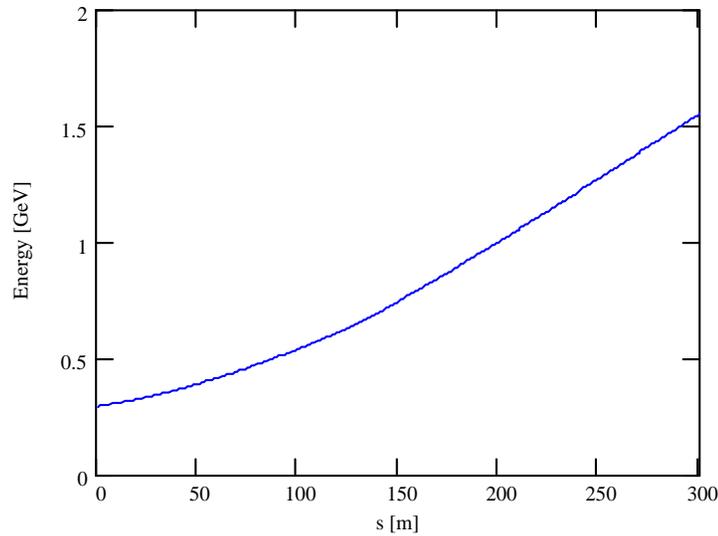


Cavity phase along the linac

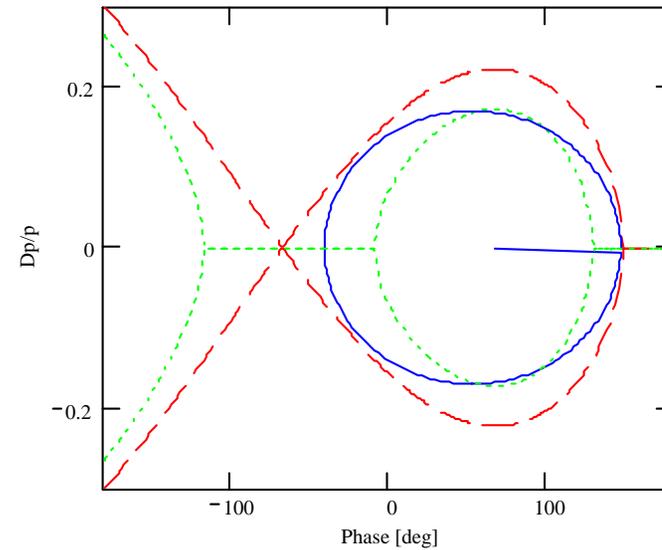


Synchrotron phase along the linac

❖ Pre-accelerator (273 MeV/c – 1.5 GeV) – Longitudinal dynamics



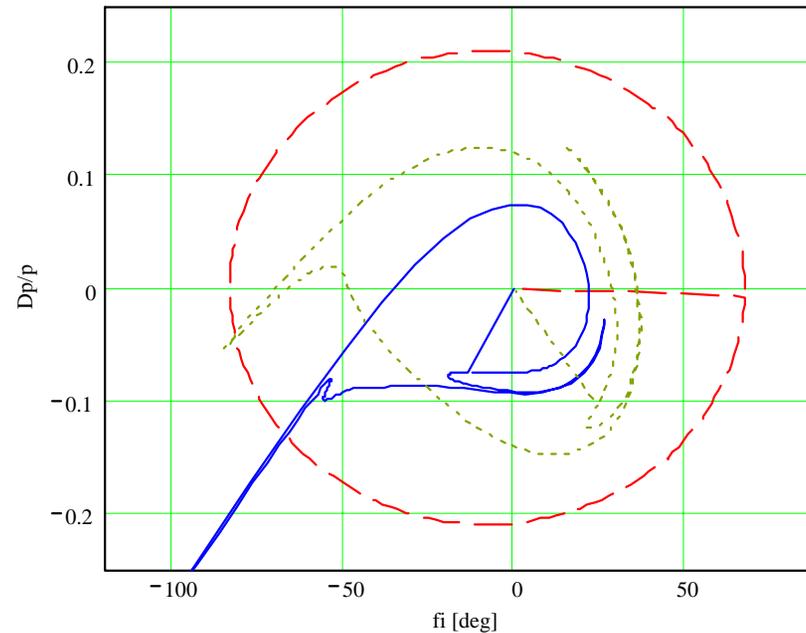
energy profile along the linac



longitudinal acceptance, bucket height

$$\Delta p/p = \pm 0.17 \text{ or } \Delta \phi = \pm 93 \text{ (200MHz)}$$

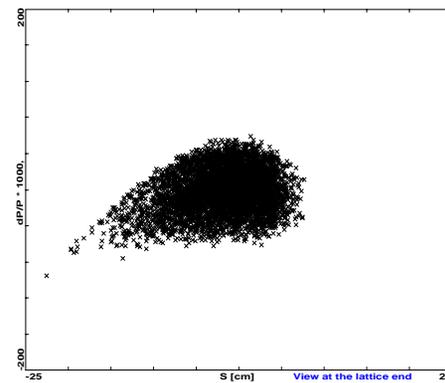
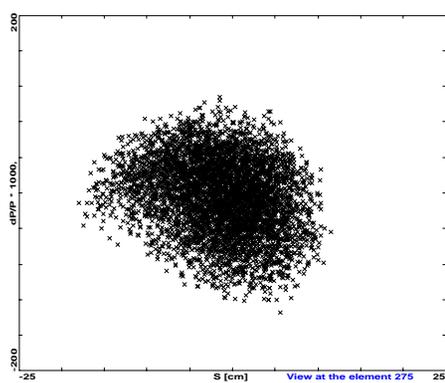
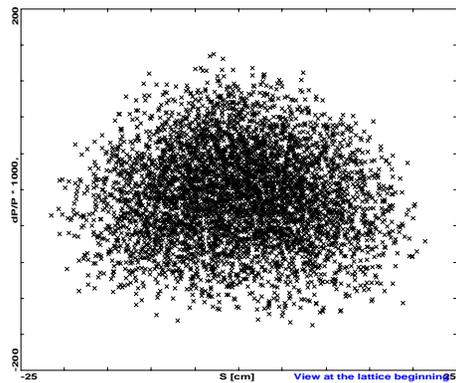
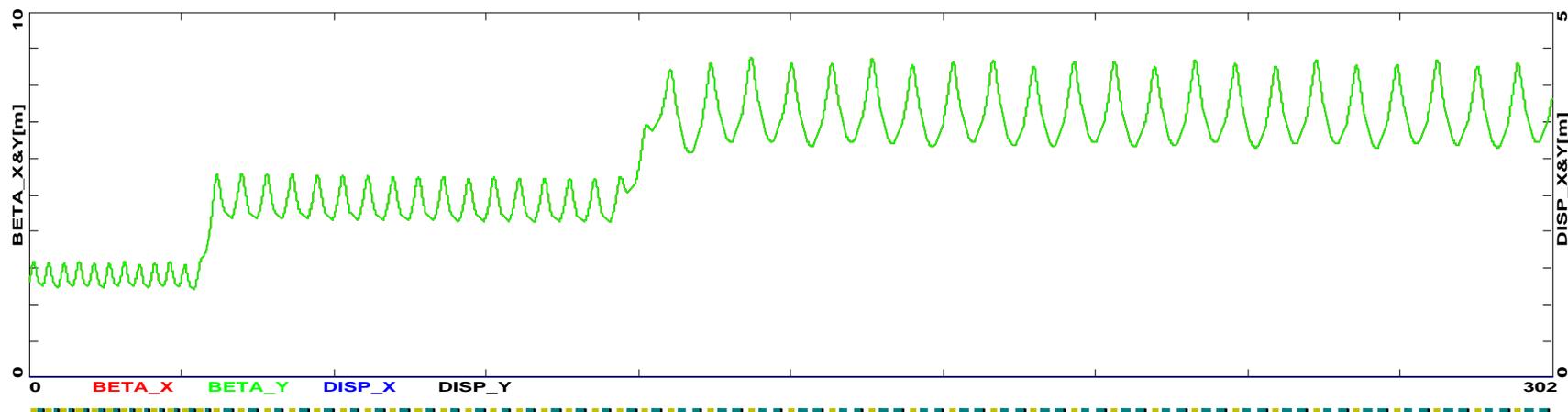
❖ Pre-accelerator (273 MeV/c – 1.5 GeV) – Longitudinal acceptance



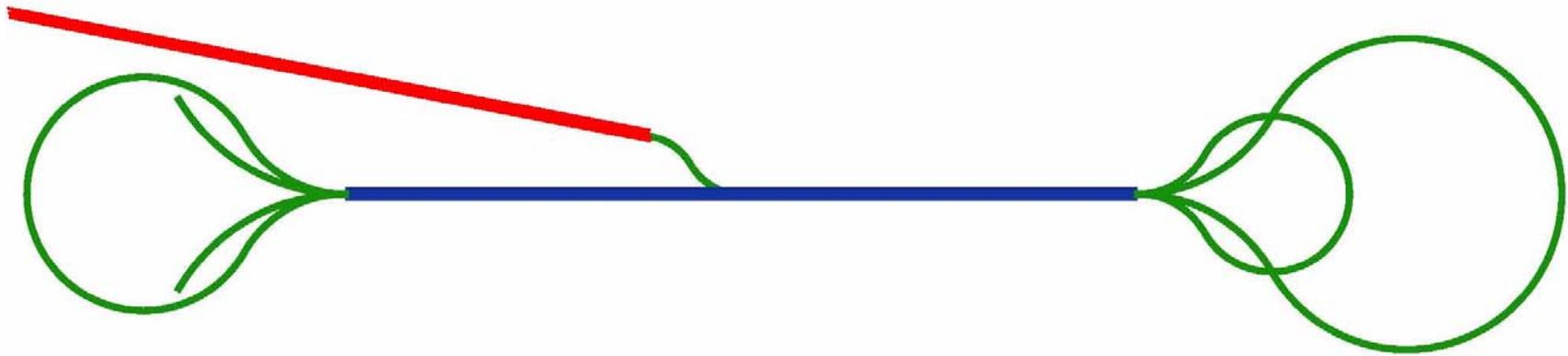
Phase space contours **before**, **half-way through** and **at the end** of acceleration – contours defined for particles at 2.5σ (95% of particles contained inside)

◆ Linear Pre-accelerator – Longitudinal dynamics, particle tracking

Fri Dec 03 09:03:52 2004 OptiM - MAIN: - D:\Study 2A\PreLinac\Linac_sol.opt

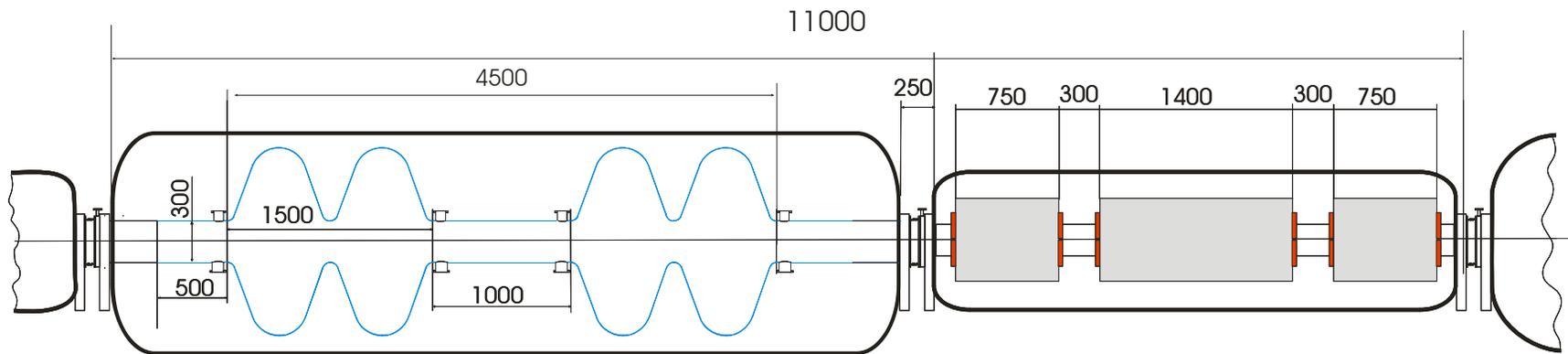


'Dogbone' RLA (3.5-pass) scheme



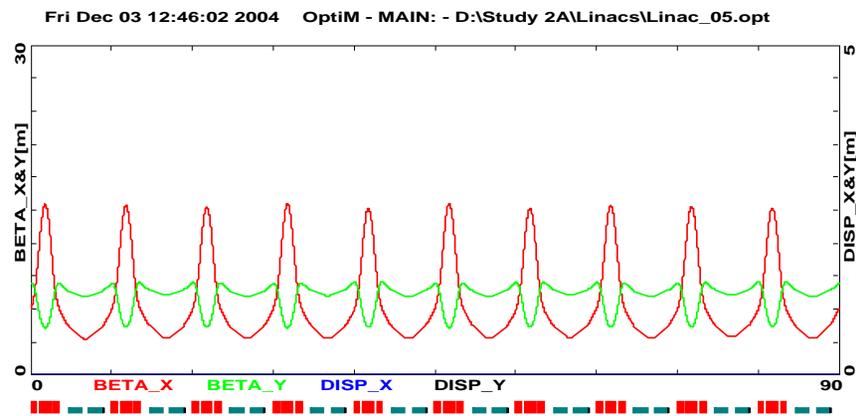
- Multi-pass linac optics
- Focusing compromise strategy
 - ◆ Focusing optimized for the **half-pass (1.5-2 GeV)** – 90° phase advance per cell
 - ◆ Uniform focusing restored in the **second half of the first full-pass (2.5-3 GeV)**

Main linac cell – long cryo-module & triplet

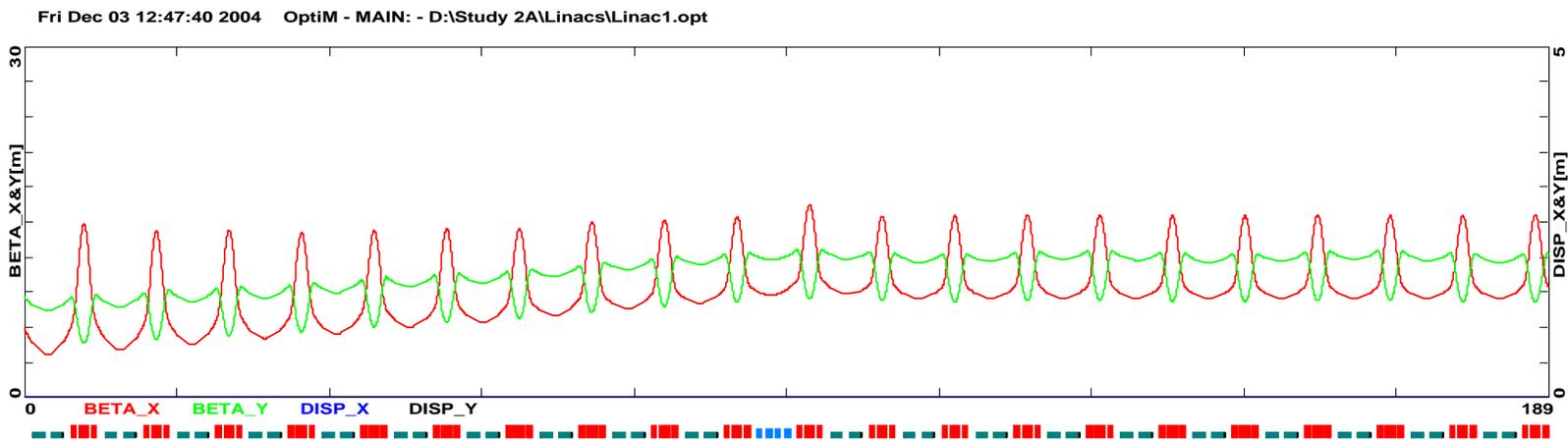


◆ Main Linac – multi-pass Optics (lower passes)

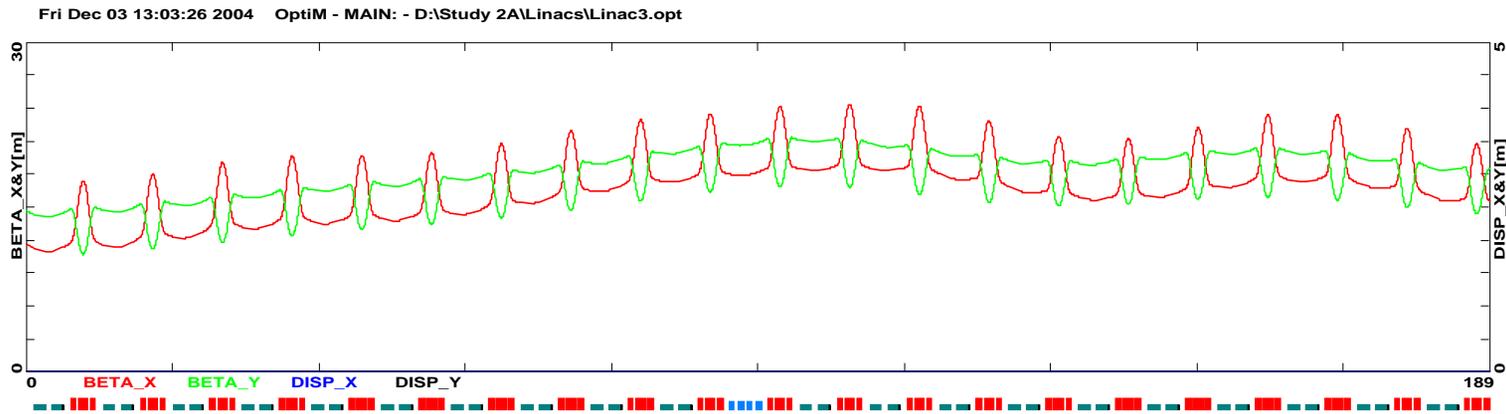
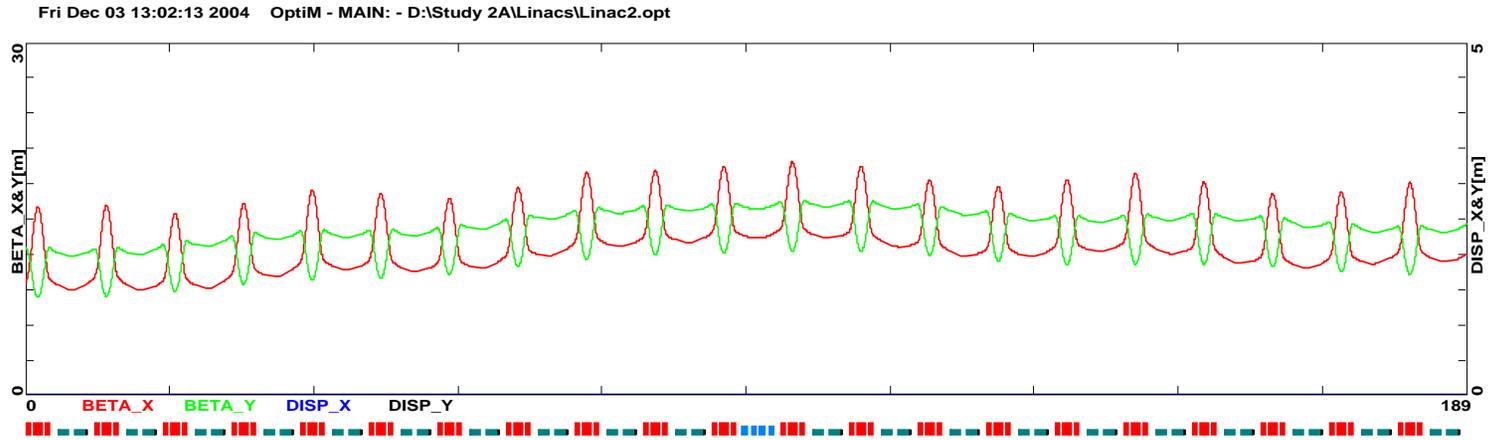
1.5-2 GeV



2-3 GeV

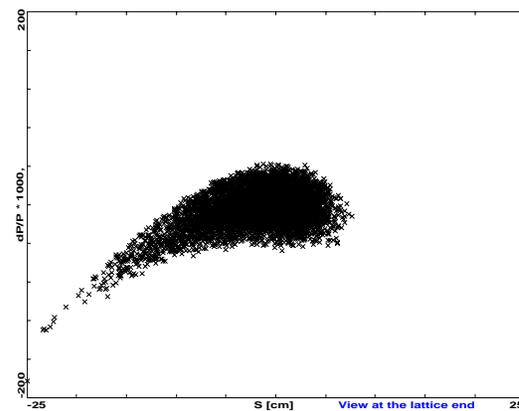
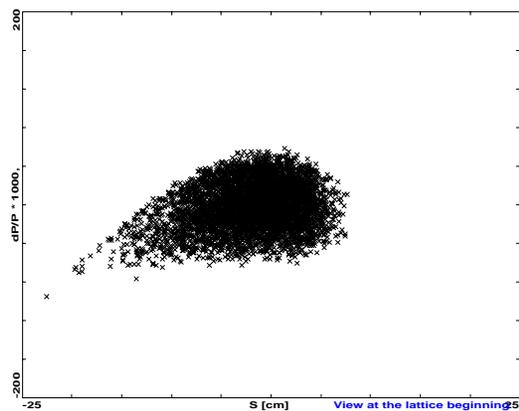
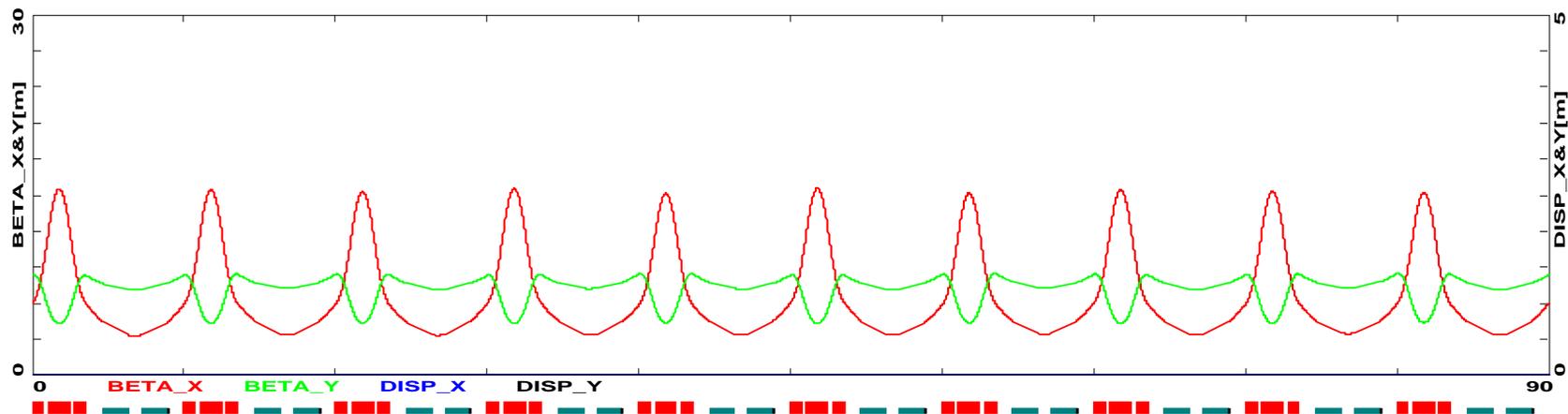


◆ Main Linac – multi-pass Optics (higher passes)



◆ Main Linac – the half-pass (1.5-2 GeV) longitudinal tracking

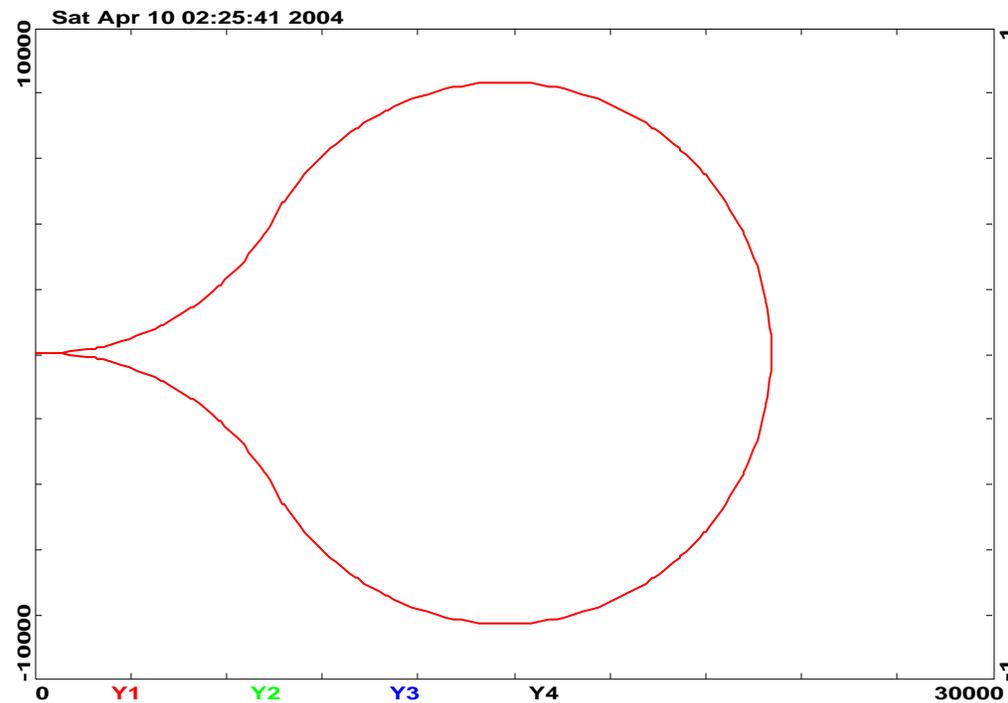
Fri Dec 03 13:11:43 2004 OptiM - MAIN: - D:\Study 2A\Linacs\Linac_05.opt



Arc Optics – beam transport choices

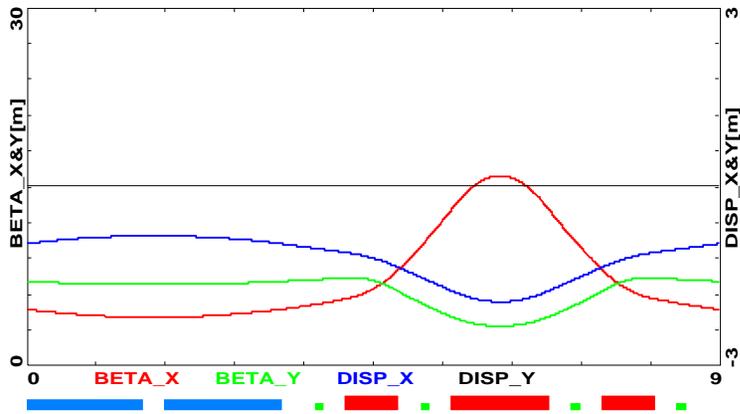
- ❖ Principle of uniform focusing periodicity (90^0) – cancellation of chromatic effects
- ❖ Single dipole (horizontal) separation of multi-pass beams in RLA
 - ◆ No need to maintain achromatic Spreaders/Recombiners
 - ◆ Compact Spreaders/Recombiners – minimized emittance dilution
- ❖ SC dipoles and quads (triplets) in RLA (1 Tesla dipoles/1 Tesla quads)
- ❖ Requirement of high periodicity and 'smooth' transition between different kinds of optics, linac-spreader-arc-recombiner-linac

❖ 'Droplet' return arc footprint (60° out – 300° in – 60° out)

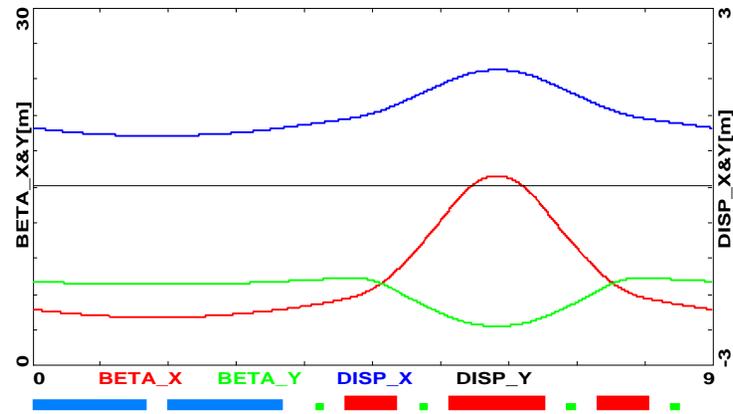


❖ 'Droplet' return arc (inward and outward cells), missing dipoles

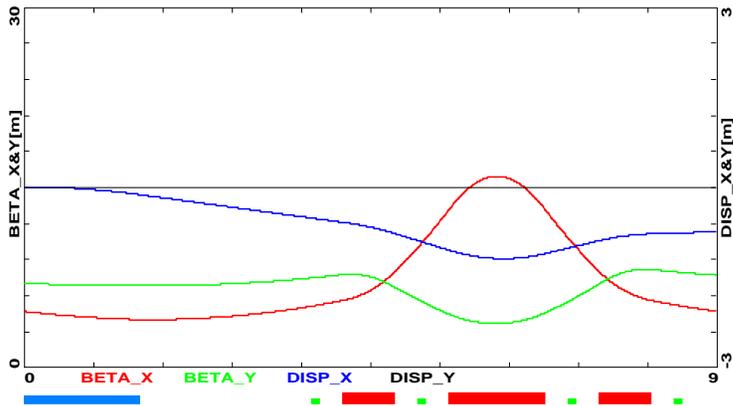
Fri Dec 03 13:23:10 2004 OptiM - MAIN: - D:\Study 2A\DropletteVA_



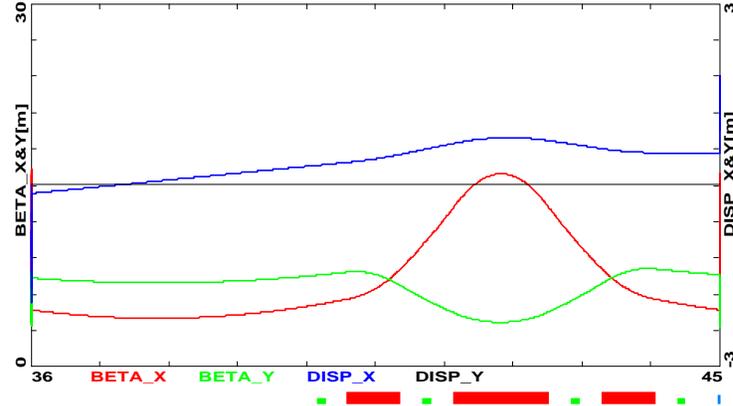
Fri Dec 03 13:24:34 2004 OptiM - MAIN: - D:\Study 2A\DropletteVA_



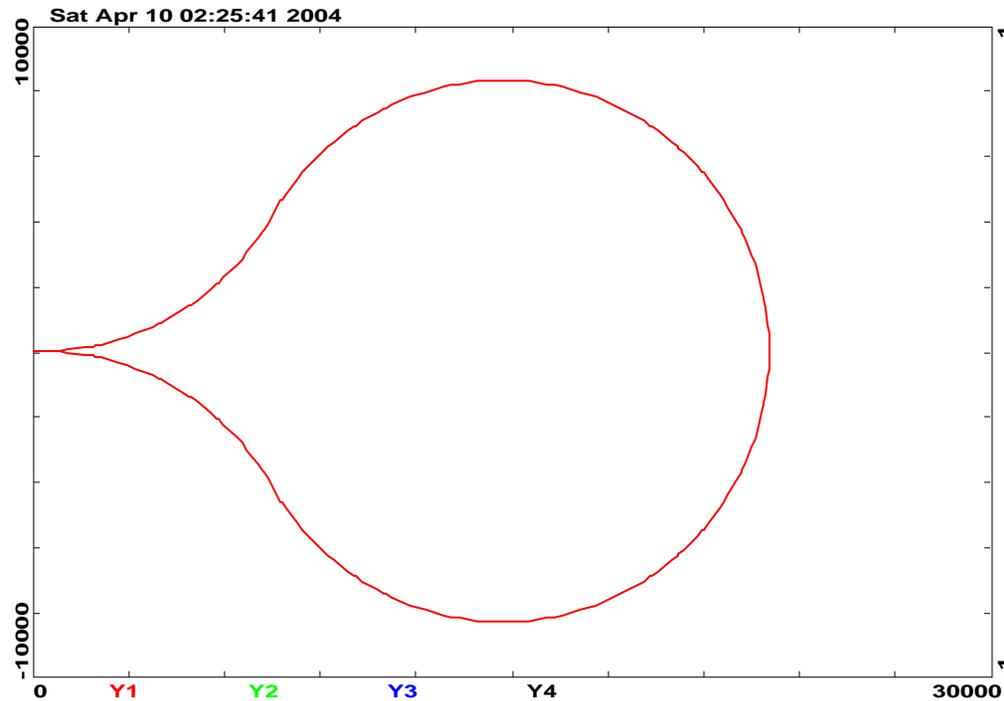
Fri Dec 03 13:27:09 2004 OptiM - MAIN: - D:\Study 2A\DropletteL_out.opt



Fri Dec 03 13:33:34 2004 OptiM - MAIN: - D:\Study 2A\Droplette\SprTr.opt

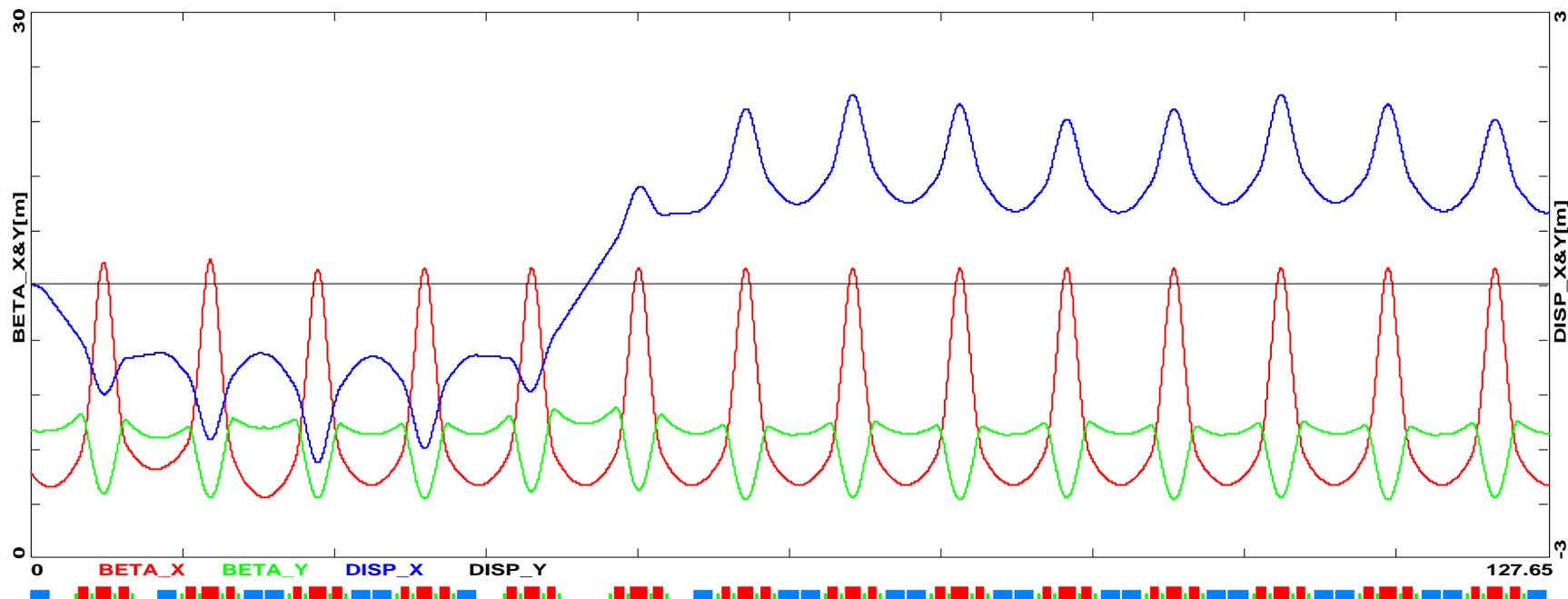


❖ 'Droplet' return arc footprint (60° out – 300° in – 60° out)



◆ 'Droplet' return half-Arc (Spreader and Transition)

Fri Dec 03 13:40:25 2004 OptiM - MAIN: - D:\Study 2A\Droplet\halfArc.opt



Dipoles:

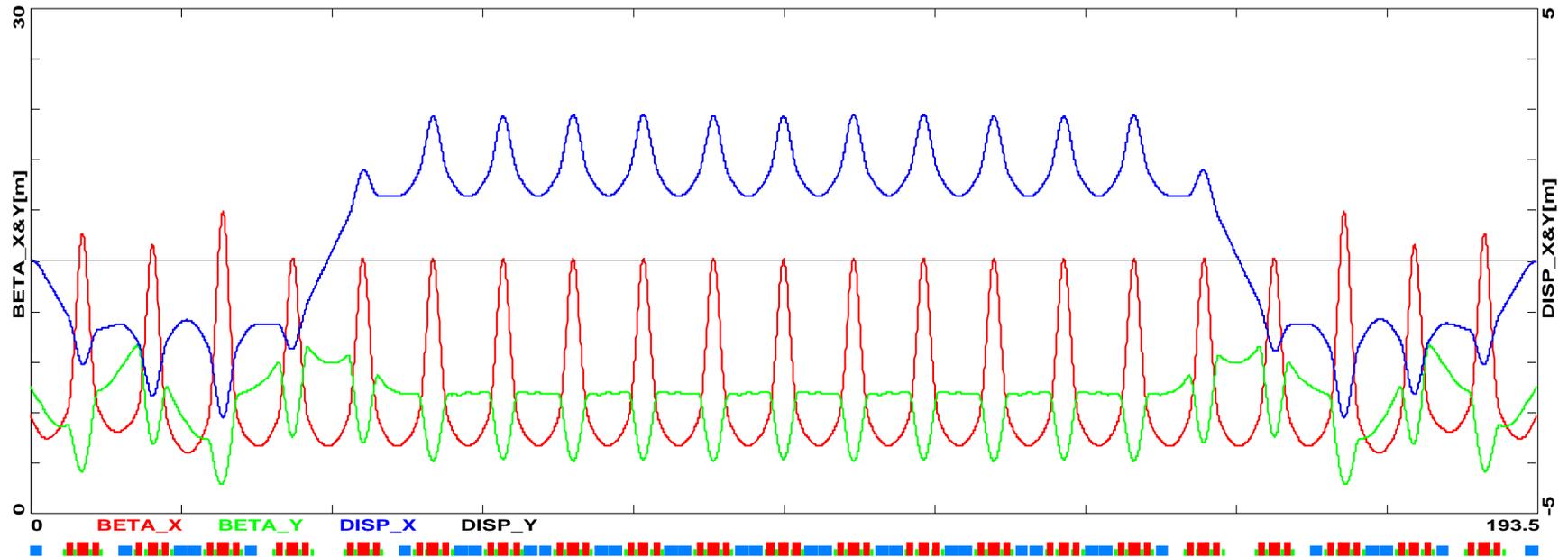
L[cm]	B[kG]
150	7.8

Quads:

	L[cm]	G[kG/cm]
D	68	-0.32
F	125	0.32

◆ 'Droplet' return Arc (matched to the linac)

Fri Dec 03 13:54:04 2004 OptiM - MAIN: - D:\Study 2A\Arcs\Arc.opt



Summary

- Ⓢ Lattice for 3.5-pass, 5 GeV, RLA based on 200MHz SRF – linear optics
 - Pre-accelerator, three styles of cryo-modules
 - Proof-of-principle Arc optics lattice – further longitudinal compression in the Arcs, with $M_{56} \sim 3$ m
 - multi-pass linac optics
 - compact Spr/Rec - 'smooth' transition of optics between linacs and Arcs
- Ⓢ Still to be demonstrated... Emittance preservation scheme – nonlinear corrections in the Arcs
 - Chromatic corrections in the Arcs to effectively restore longitudinal space linearity (via three families of sextupoles)
 - Emittance preservation checked independently by ICOOL