

**B Production and ONIUM  
Production  
at the Tevatron**

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(for the CDF and DØ Collaborations)**

**HQ98 Workshop  
Fermilab  
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## Outline (B Production)

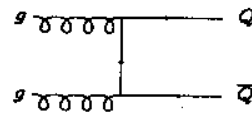
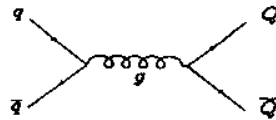
- Introduction
- Brief Summary of “old” Results
- Forward  $\mu$  and *b*-Quark Production (DØ)
  - Analysis procedure
  - Inclusive  $\mu$  cross section
  - *b*-produced  $\mu$  cross section
  - Rapidity dependence
- $b\bar{b}$  Rapidity Correlations (CDF)
  - Analysis procedure
  - Ratio forward–central / central–central
  - Probing the gluon distribution
- Outlook

# $b\bar{b}$ production in pQCD

$$\mathcal{O}(\alpha_s^3) \sim \mathcal{O}(\alpha_s^2)$$

$$\mathcal{O}(\alpha_s^2) \rightarrow$$

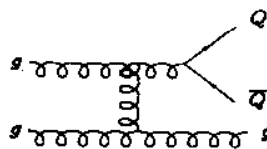
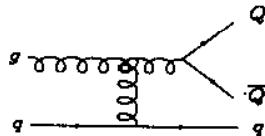
Flavor Creation



$\mathcal{O}(\alpha_s^2)$  (a)

$$\mathcal{O}(\alpha_s^3) \rightarrow$$

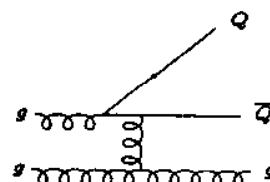
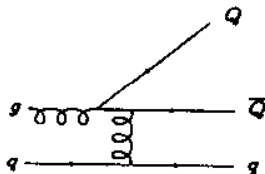
Gluon Splitting



$\mathcal{O}(\alpha_s^2)$  (b)

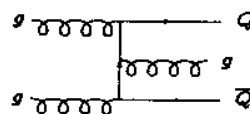
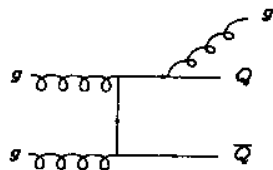


Flavor Excitation



$\mathcal{O}(\alpha_s^2)$  (c)

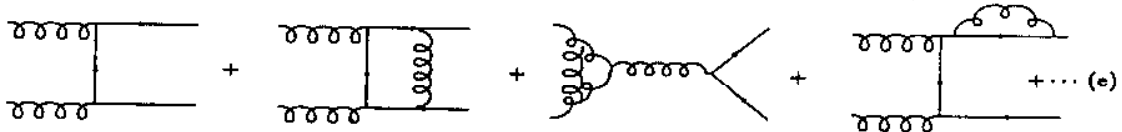
Gluon Radiation



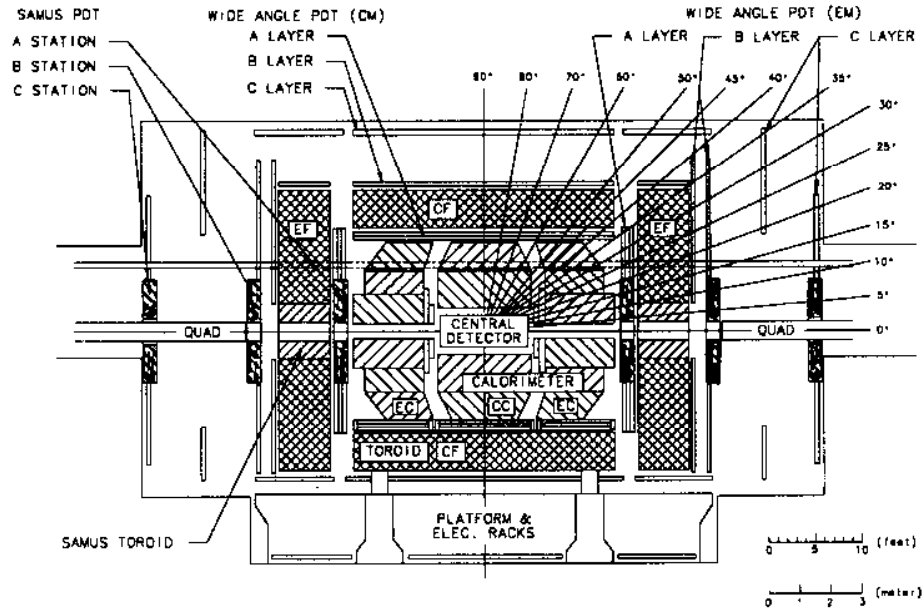
$\mathcal{O}(\alpha_s^2)$  (d)

Interference Terms

$\mathcal{O}(\alpha_s^2)$  with  $\mathcal{O}(\alpha_s^1)$  virtual graphs  $\Rightarrow \mathcal{O}(\alpha_s^3)$



## DØ Muon Spectrometer



- **Wide Angle Muon System (WAMUS)**

- Coverage:  $|\eta^\mu| < 2.4$        $\eta = -\ln(\tan(\theta/2))$
  - in these analyses:  $|\eta^\mu| < 0.8$
  - Momentum resolution:
- $$\Delta p/p = \sqrt{(0.18)^2 + (0.008p)^2} \quad (p \text{ in GeV}/c)$$

- **Small Angle Muon System (SAMUS)**

- Coverage:  $1.7 < |\eta^\mu| < 3.3$
- in these analyses:  $2.4 < |\eta^\mu| < 3.2$
- Momentum resolution:

$$\begin{aligned} \Delta p/p &= 19\% \text{ at } p = 20 \text{ GeV}/c \\ &= 25\% \text{ at } p = 100 \text{ GeV}/c \end{aligned}$$

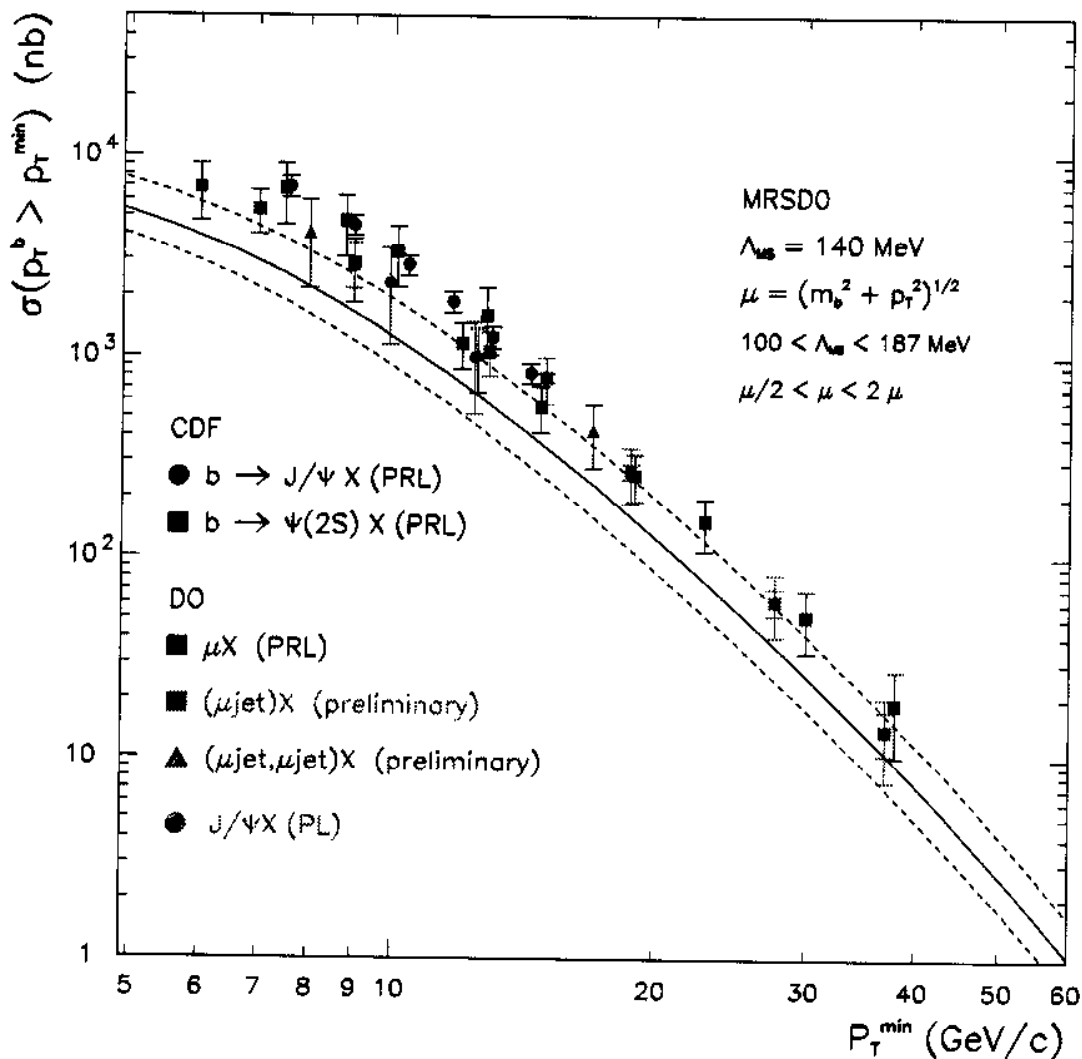
## Beauty Production in Hadron Collisions

### Motivation

- Test of perturbative QCD
  - *b* production has been calculated in pQCD to next-to-leading order ( $\mathcal{O}(\alpha_s^3)$ ):
    - \* P. Nason, S. Dawson and R. K. Ellis
    - \* W. Beenakker, W. L. van Neerven, R. Meng, G. A. Schuler and J. Smith
    - \* M. Mangano, P. Nason, G. Ridolfi
  - NLO  $\sim$  LO
  - (running)  $\alpha_s$  measurement
- Probe gluon densities ~~at small  $x$ , below DIS range~~
- Heavy quarkonium production mechanisms
- Gluon fragmentation ( $\mu$ 's in jets)
- Reliable predictions of *b* cross-section for future experiments (CP violation,  $B_s$  mixing, rare decays)

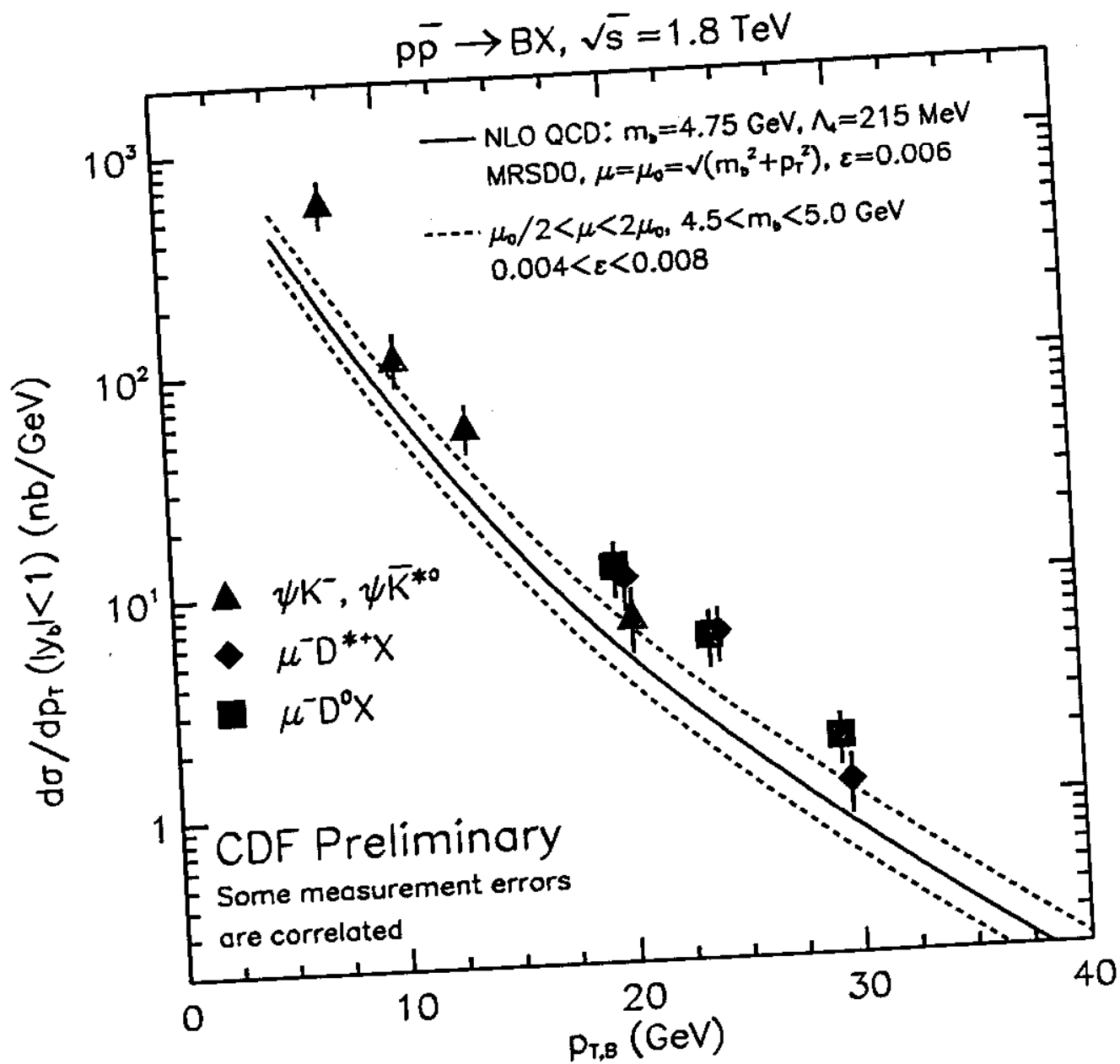
## *b*-Quark Production in Central Region

- Inclusive *b*-Quark production cross section at  $\sqrt{s} = 1.8$  TeV for  $|y^b| < 1$ :



⇒ Data/Theory:

- $\approx 2.1$  DØ ⇒ ( $\approx 2.5$  with ISAJET 7.37)
- $\approx 2.8$  CDF



## Inclusive Forward *b* Production (DØ)

- Analysis based on Small Angle Muon System (SAMUS).

- 3 layers of drift tubes
- Toroidal magnet between first and second layer
- Coverage:  $2.2 < |\eta^\mu| < 3.3$      $\eta = -\ln(\tan(\theta/2))$
- Momentum resolution (*p* in GeV/*c*):

$$\Delta p/p = \sqrt{\left(0.25 \frac{p - 5.3}{p}\right)^2 + (0.21 p)^2}$$

- Special 1994-95 runs —  $\int \mathcal{L} dt = 111 \pm 6 \text{ nb}^{-1}$

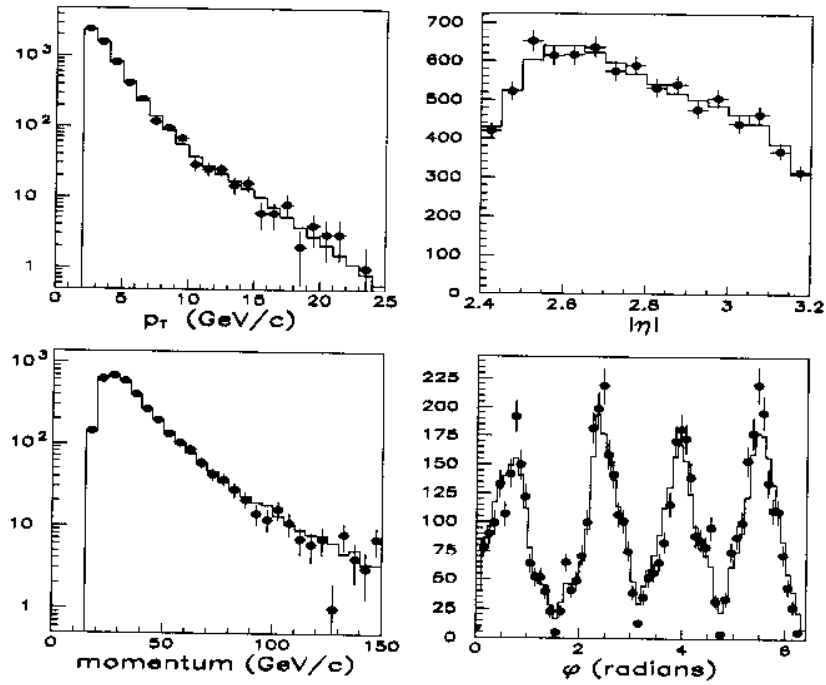
- $2.4 < |\eta^\mu| < 3.2$
- $p_T^\mu > 2 \text{ GeV}/c$
- $p^\mu < 150 \text{ GeV}/c$
- Quality cuts
- Calorimeter confirmation
- Single interaction events

⇒ 6709 events

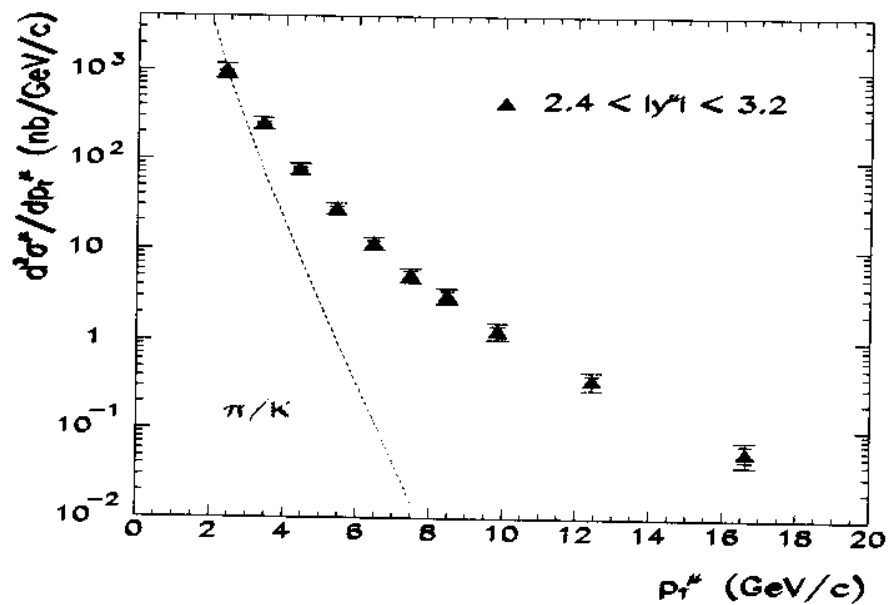


## Inclusive Muon Cross Section

- Muon detection efficiencies determined with MC
- Reconstructed MC distributions match data:



- Unfolded  $p_T$  spectrum of forward muons:

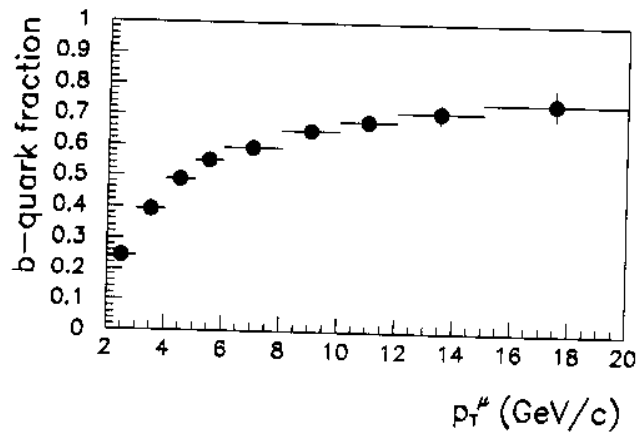


## Extraction of *b*-Quark Contribution

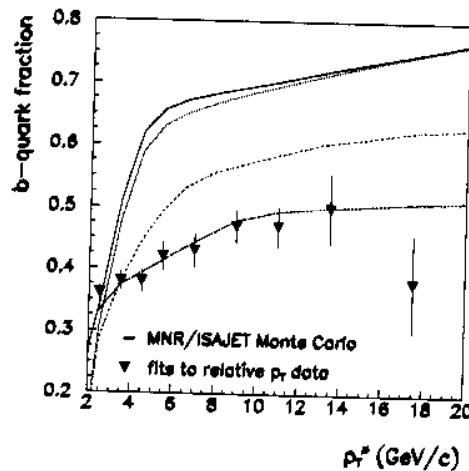
- Contribution from  $\pi/K \rightarrow \mu$  taken from ISAJET.
- Use fraction of muons due to *b*-quark decays

$$f_b = \frac{\sigma(b \rightarrow \mu)}{\sigma(b \rightarrow \mu) + \sigma(c \rightarrow \mu)}$$

as predicted by NLO QCD (MNR).



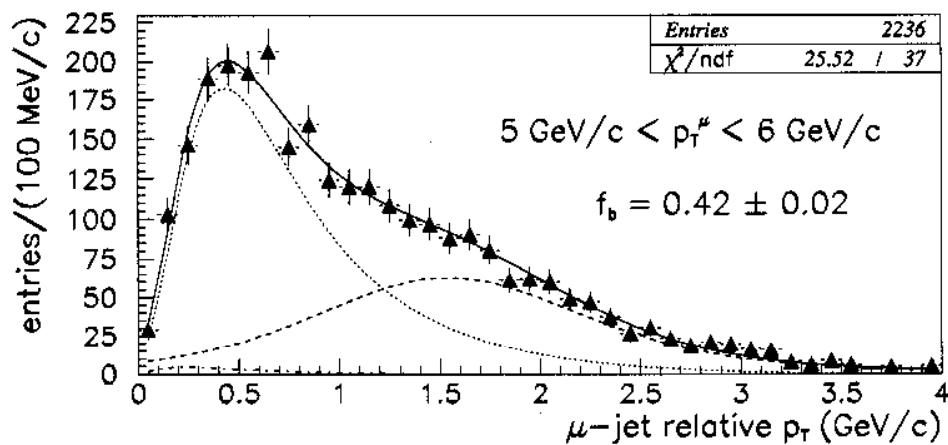
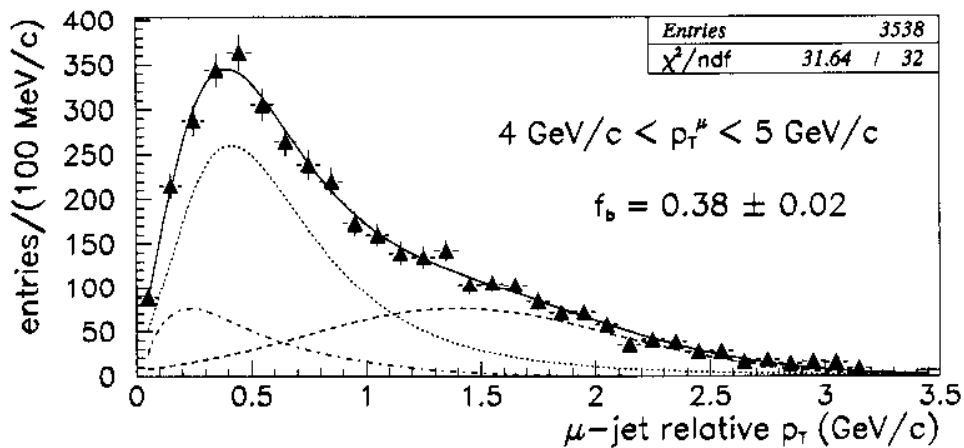
- $f_b$  for muon+jet events using  $p_T^{\text{rel}}$  fits.



⇒ Good agreement between data and QCD predictions.

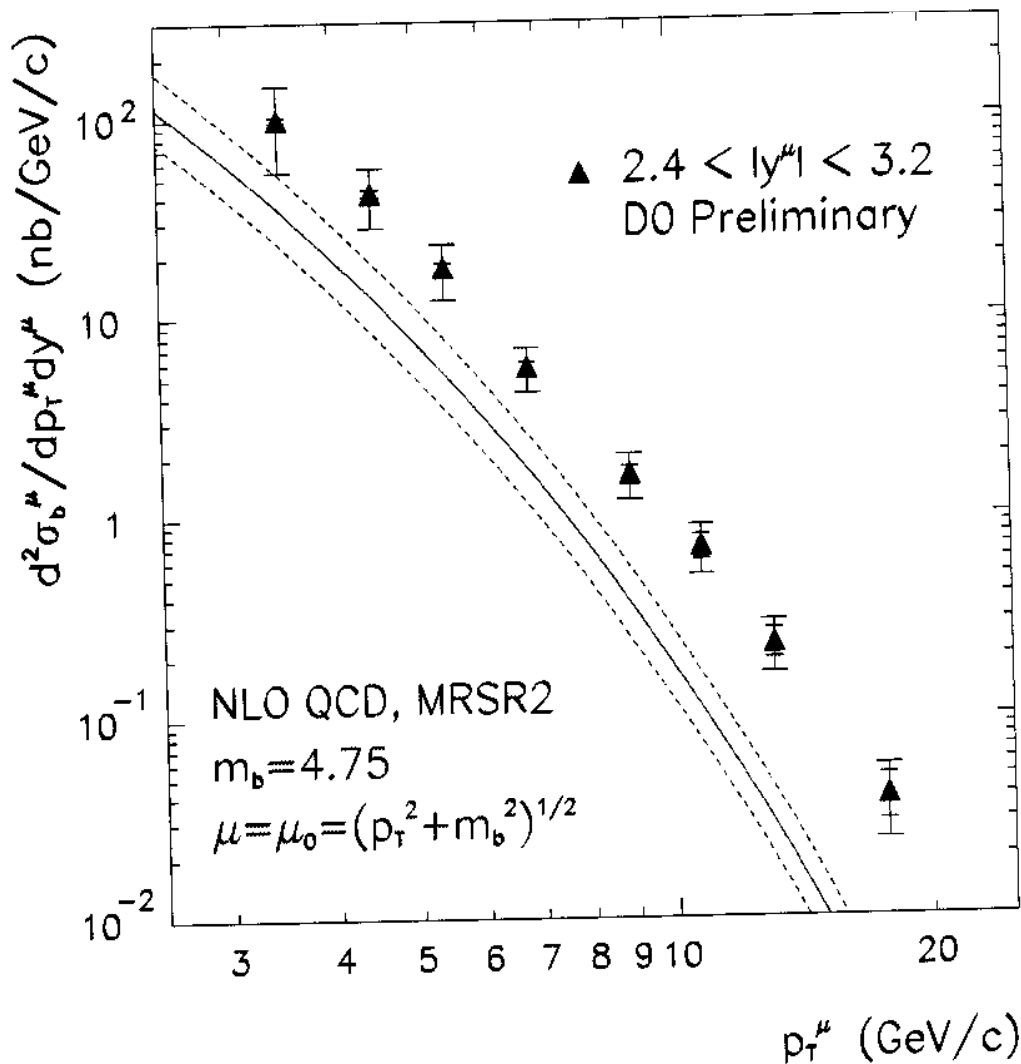
## *b*-Fraction Cross Check

- Determine  $f_b$  for events with a reconstructed associated jet (7% of the muon sample):
  - Use all Run 1B data —  $\int \mathcal{L} dt = 90 \text{ pb}^{-1}$
  - no trigger requirement  $\Rightarrow$  20,000 events.
  - Shape of  $p_T^{\text{rel}}$  distributions obtained from real data ( $\pi/K$ ) or ISAJET (*b* and *c* quarks).
  - Muons from  $b \rightarrow c \rightarrow \mu$  included in the *c*-quark sample.
  - $p_T^{\text{rel}}$  fits for  $p_T^\mu$  bins.



## *b*-Produced Muon Cross Section

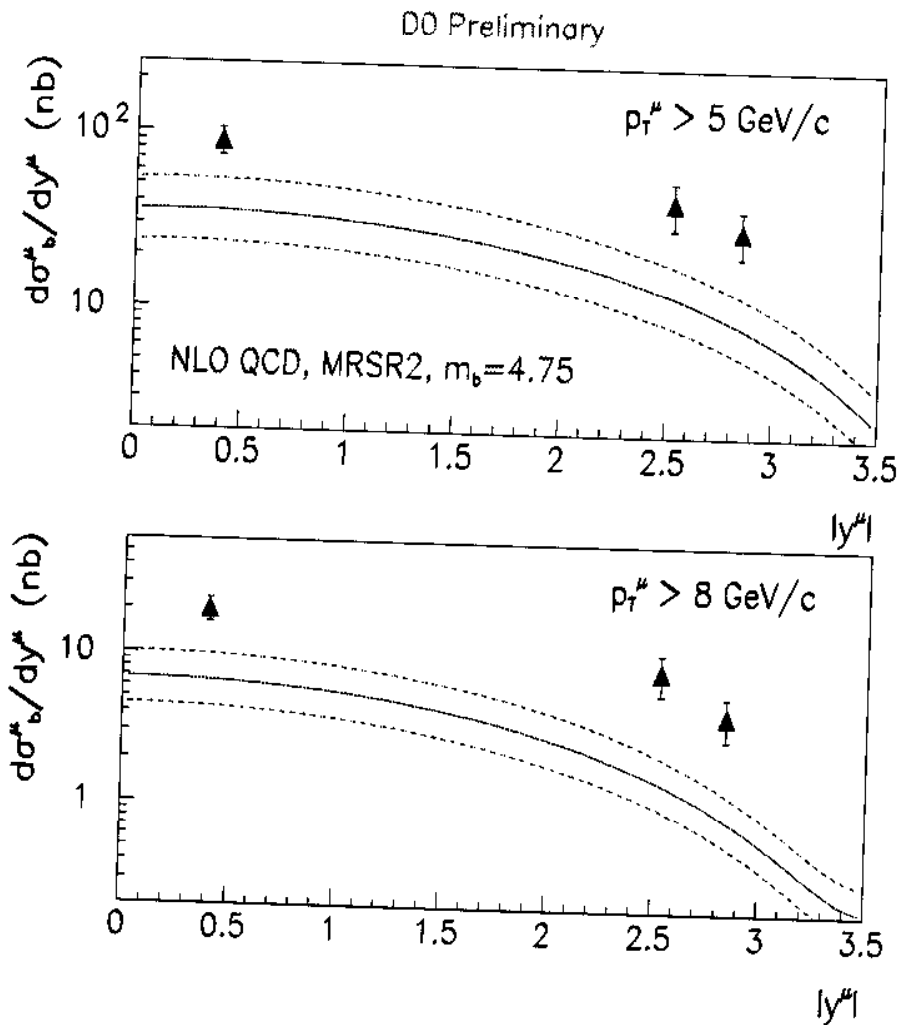
- $p_T$  spectrum of forward muons from *b* decays compared to NLO QCD prediction (HVQJET).



⇒ Measured cross section  $\approx$  4 times higher than NLO QCD prediction.

## Rapidity Dependence

- *b*-produced muon cross section *vs.* rapidity compared to the NLO QCD prediction:



⇒ Ratio Data/Theory ( $p_T^\mu > 5 \text{ GeV}/c$ ):

–  $2.5 \pm 0.5$       $|y^\mu| < 0.8$

–  $3.6 \pm 0.9$       $2.4 < |y^\mu| < 3.2$

## Recent Theoretical Studies

- "Variable Flavor Number" scheme

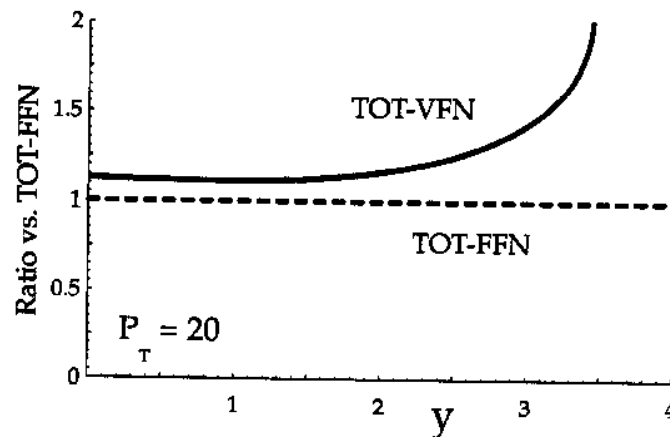
(F.I Olness, R.J. Scalise, and Wu-Ki Tung, hep-ph/9712494)

- Usual QCD parton formalism:  $m_Q = 0$  when  $p_T > m_Q \Rightarrow$  *zero-mass variable-flavor-number* scheme
- NLO QCD calculations: Q is always a heavy particle  $\Rightarrow$  *fixed-flavor-number* scheme (FFN)
- New development: retains the  $m_Q$  dependence at all energy scales  $\Rightarrow$  *general-mass variable-flavor-number* scheme (VFN).

Initial- and final-state mass singularities associated with heavy quark mass resummed into parton distributions, without taking the zero mass limit on the hard cross section.

### Implications:

- Enhanced cross section for *b* production
- Broader rapidity distribution



## Recent Theoretical Studies — cont.

- Hadronization of the heavy quark

*b* → *B* fragmentation function used with NLO evaluation of the *b* cross section should be harder than the commonly used Peterson f.f. with  $\epsilon_b = 0.006$ .

Example: Colangelo–Nason fragmentation function:

$$f(z) \propto (1 - z)^\alpha z^\beta$$

Implications:

- $\approx 30\%$  ( $40\%$ ) higher predicted *B* cross section in the central (forward) region.

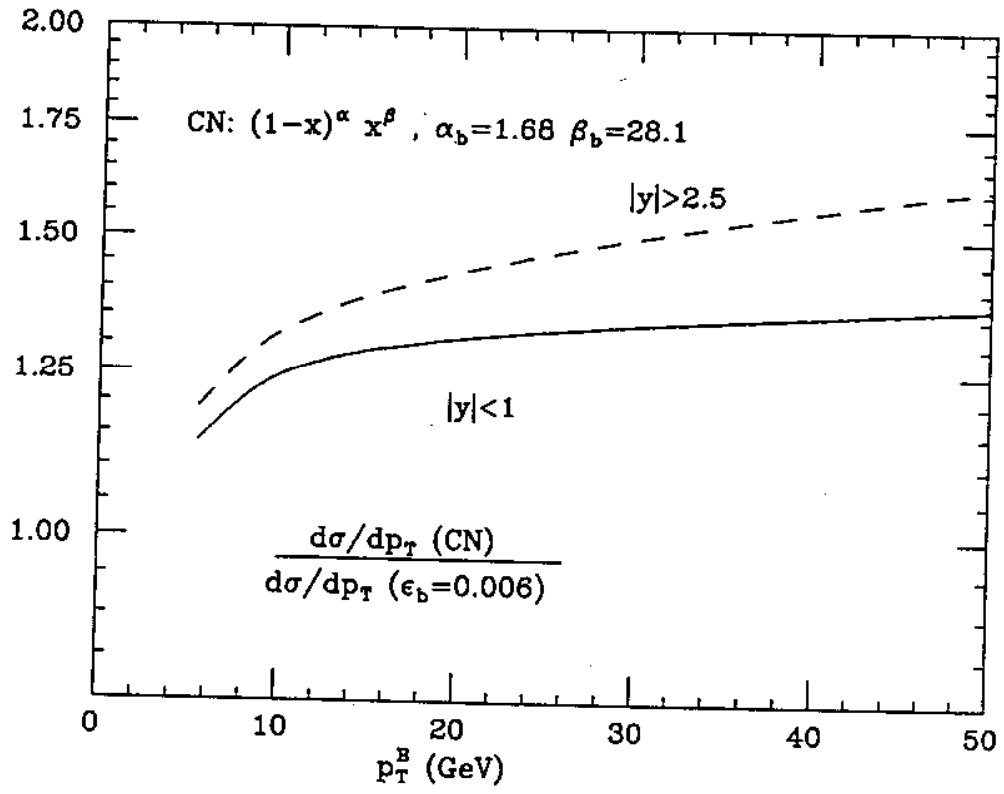
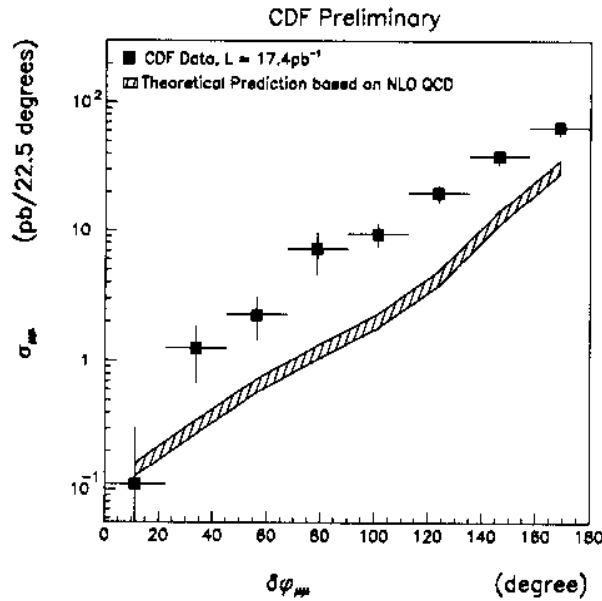


Figure 24: Ratio of the B-meson  $p_T$  distribution using the Colangelo-Nason fragmentation function (with the parameters  $\alpha$  and  $\beta$  fitted at NLO), relative to that obtained by using the Peterson fragmentation function and  $\epsilon_c = 0.06$ . Central production (solid) and forward production (dashes).



## *b* $\bar{b}$ Rapidity Correlations (CDF)

- Study of *b* $\bar{b}$  correlation is fundamental to test NLO QCD predictions.
- Previous studies based on  $\Delta\phi_{b\bar{b}}$  or  $\Delta\phi_{\mu\mu}$ :



- CDF measurement of correlated central–forward *b* $\bar{b}$  production:

$$\sigma(p\bar{p} \rightarrow b\bar{b}) = 6.49 \pm 0.63(\text{stat})_{-1.23}^{+1.43}(\text{syst}) \text{ nb}$$

with  $p_T(b, \bar{b}) > 25 \text{ GeV}/c$

$$|\eta(b_1)| < 1.5$$

$$1.8 < |\eta(b_2)| < 2.6$$

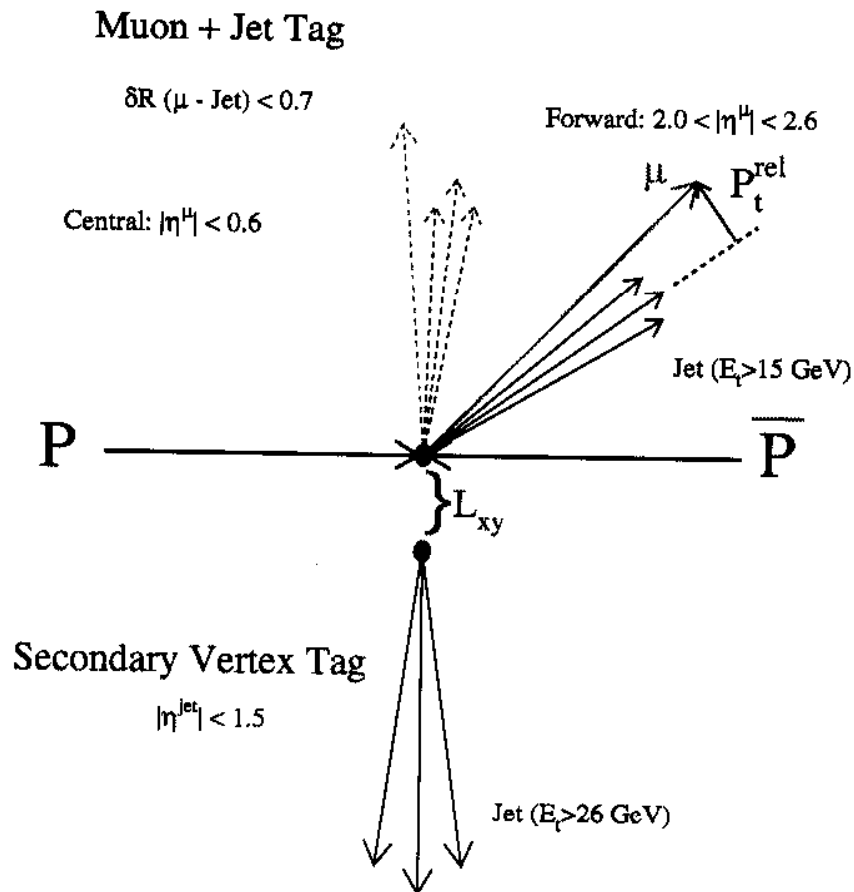
- Data / NLO QCD  $\approx 2.4$ .
- This analysis:

$$\frac{\sigma_{b\bar{b}}(\text{central} - \text{forward})}{\sigma_{b\bar{b}}(\text{central} - \text{central})}$$

## Analysis Method

- Select events with:

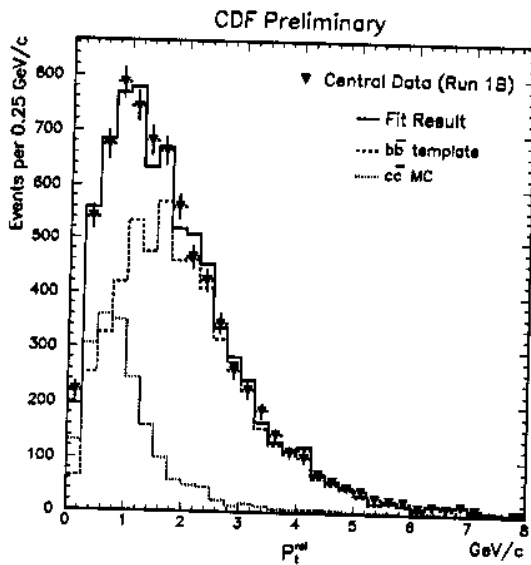
- central *b*-quark jet ( $|\eta^{\text{jet}}| < 1.5$ ) with a displaced secondary vertex.
- second *b*-quark decaying to muon+jet and produced in the central ( $|\eta^\mu| < 0.6$ ) or forward ( $2.0 < |\eta^\mu| < 2.6$ ) rapidity regions.



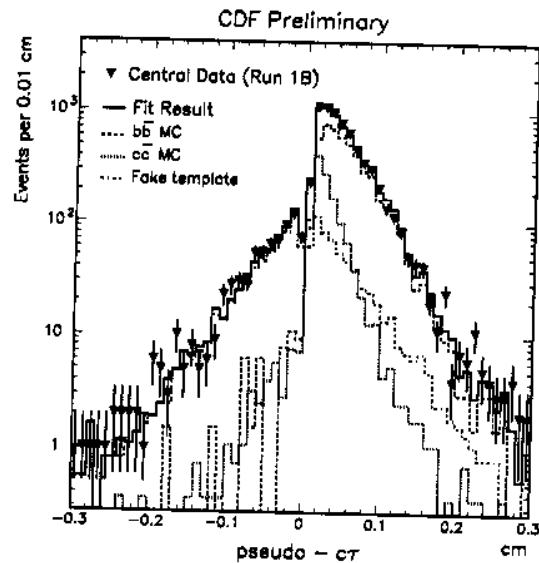
- 1994–95 Tevatron run ( $\int \mathcal{L} dt = 80 \text{ pb}^{-1}$ )  
 $\Rightarrow$  382 forward–central events  
 7544 central–central events

## Signal Extraction

- Signal fraction extracted by simultaneous fits of the  $p_T^{\text{rel}}$  of the muon and the pseudo- $c\tau$  of the *b*-jet.
- Central-central events:



$p_T^{\text{rel}}$  distribution



pseudo- $c\tau$  distribution

Source ( <i>b</i> -tag/ $\mu$ -tag)	forward-central	central-central
Real <i>b</i> / Real <i>b</i>	$0.739 \pm 0.073$	$0.582 \pm 0.021$
<i>c</i> / $\bar{c}$	$0.123 \pm 0.089$	$0.169 \pm 0.021$
Real <i>b</i> / Fake	$0.034^{+0.087}_{-0.034}$	$0.085 \pm 0.026$
Fake / Real <i>b</i>	$0.104 \pm 0.030$	$0.165 \pm 0.009$

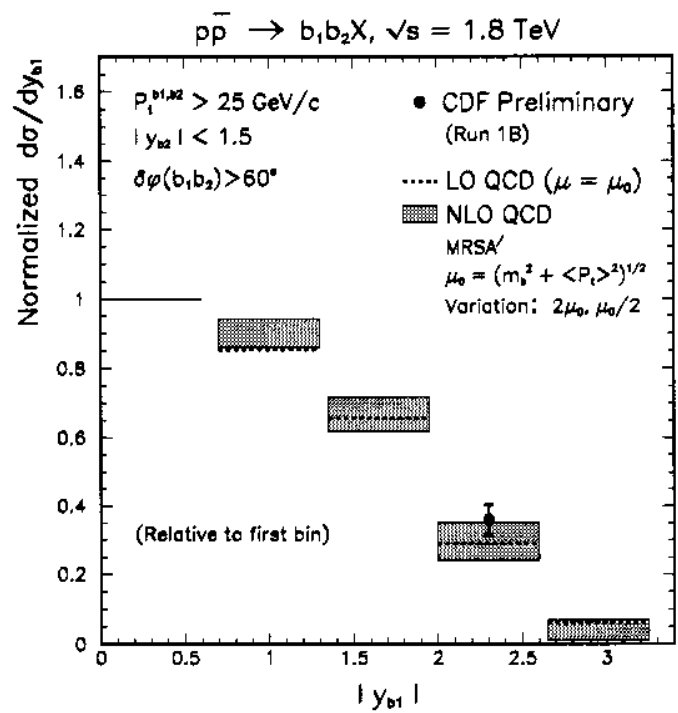
## Cross Section Ratio

$$R_{\text{data}} = \frac{\sigma(pp \rightarrow b_1 b_2 X; 2.0 < |y_{b_1}| < 2.6)}{\sigma(pp \rightarrow b_1 b_2 X; |y_{b_1}| < 0.6)}$$

where:  $p_T(b_1, b_2) > 25 \text{ GeV}/c$ ,  
 $|y_{b_2}| < 1.5$ ,  
 $\delta\phi(b\bar{b}) > 60^\circ$ .

$$R_{\text{data}} = 0.361 \pm 0.041(\text{stat})_{-0.023}^{+0.011}(\text{syst})$$

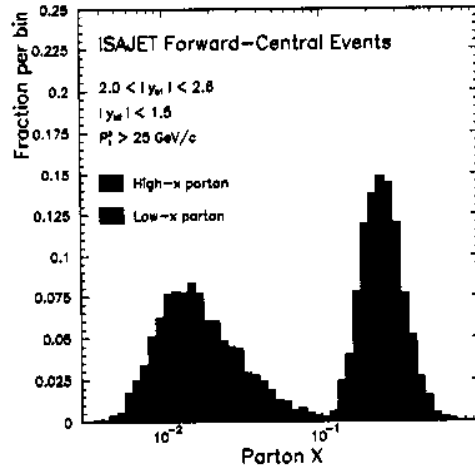
$$R_{\text{theory}} = 0.338_{-0.097}^{+0.014}$$



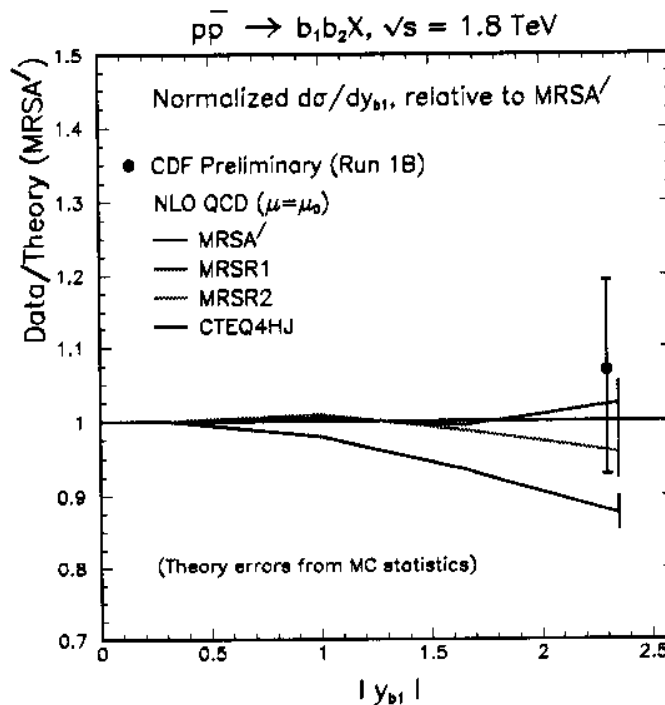
## Probing the Gluon Distribution

- Forward–central events correspond to

$$x_{\text{low}} \approx 0.025 \quad x_{\text{high}} \approx 0.25$$



- Sensitivity to  $G(x, Q^2)$  at large  $x$  values.
- Comparison of  $R_{\text{data}}$  with  $R_{\text{theory}}$  obtained from various parton distribution functions.

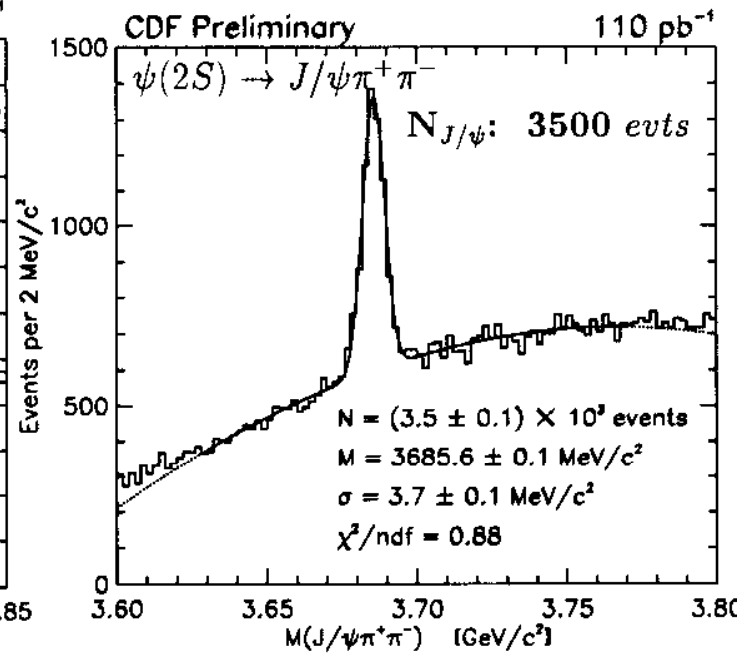
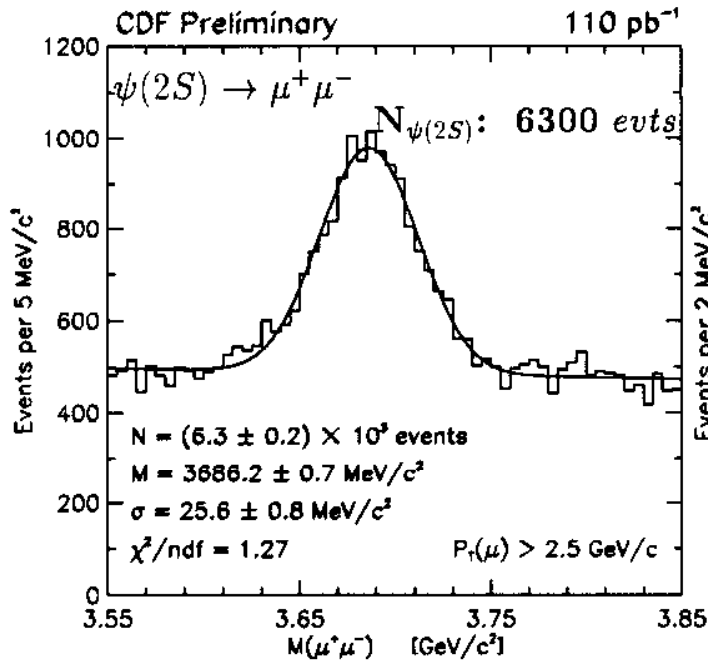
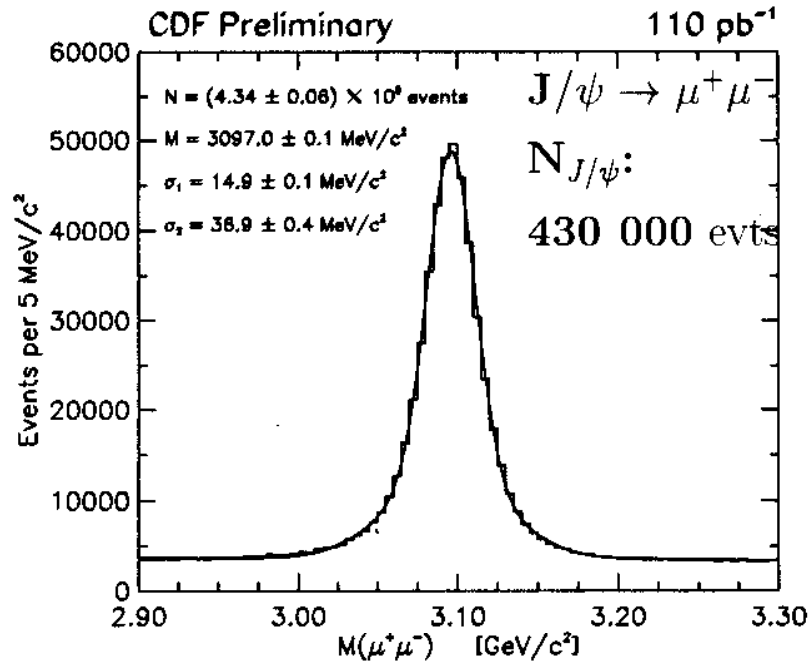


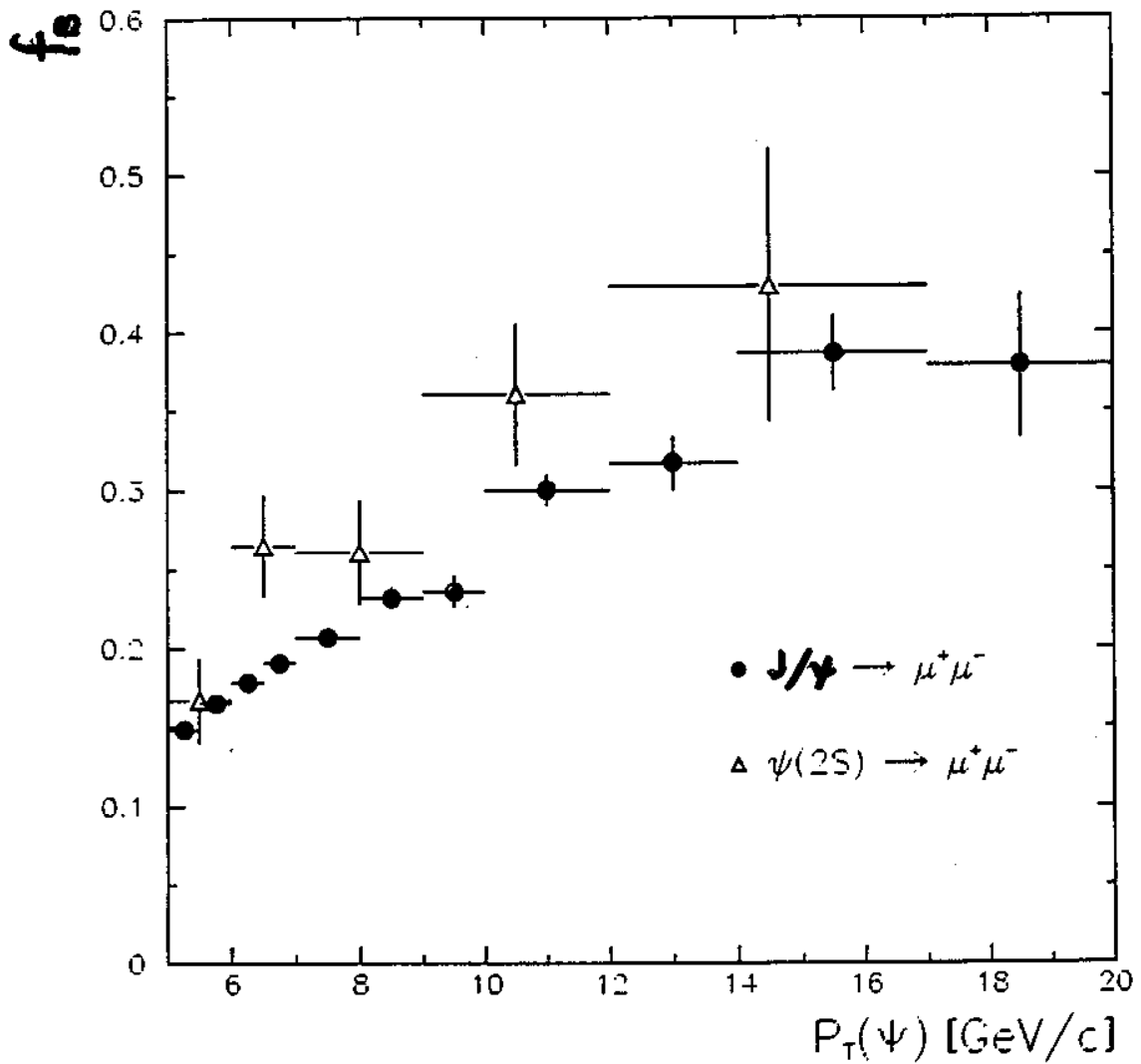
## Overview of Quarkonium Production

- Provides insight into the nature of strong interactions. Window on the boundary region between perturbative and non-perturbative QCD.
- Processes involved:
  - Prompt production: (primary vertex):
    - \* direct
    - \* indirect e.g.  $\chi_c \rightarrow J/\psi\gamma$
  - b-quark decays (secondary vertex)
- Recently Published/Available Results on ONIA Production::
  - $\Upsilon$  cross section (CDF)  
PRL 75, 4358 (1995).
  - Central  $J/\psi$  cross section,  $f_b$ ,  $f_\chi$  (DØ),  
PL B370, 239(1996).
  - Central  $J/\psi$ ,  $\psi(2s)$  cross section,  $f_b$  (CDF),  
PRL 79, 572(1997).
  - Production of  $J/\psi$  from  $\chi_c$  (CDF),  
PRL 79, 578(1997).
  - Forward  $J/\psi$  Production ((DØ);  
submitted to PRL
  - Measurement of the Ratio of Production of  $\chi_{c1}$   
to  $\chi_{c2}$  (CDF) - preliminary

# Charmonium Production at CDF

● Full Run I charmonium statistics.





The fractions of  $J/\psi$  and  $\psi(2S)$  originating  
from  $b$ -hadron decays



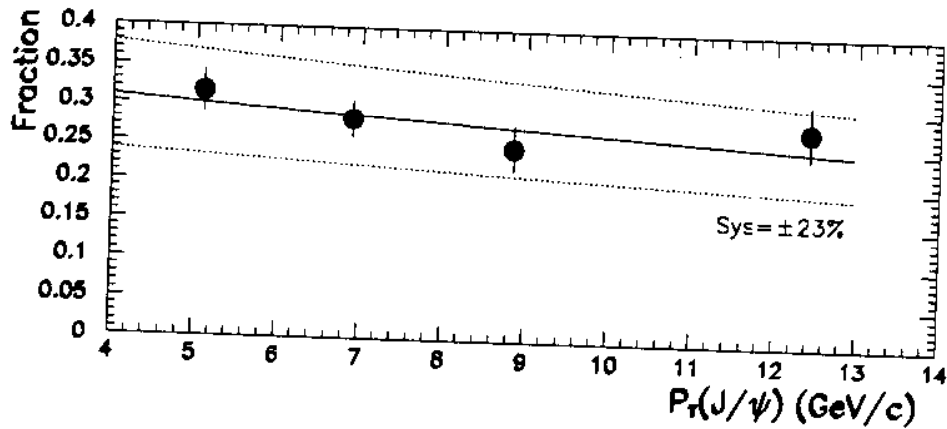
# χ<sub>c</sub> Production at CDF

## ● Removing B → J/ψ X and B → χ<sub>c</sub> X

- Analysis of the Transverse Decay Length;
- Fractions of χ<sub>c</sub> from B → J/ψ and J/ψ from B.

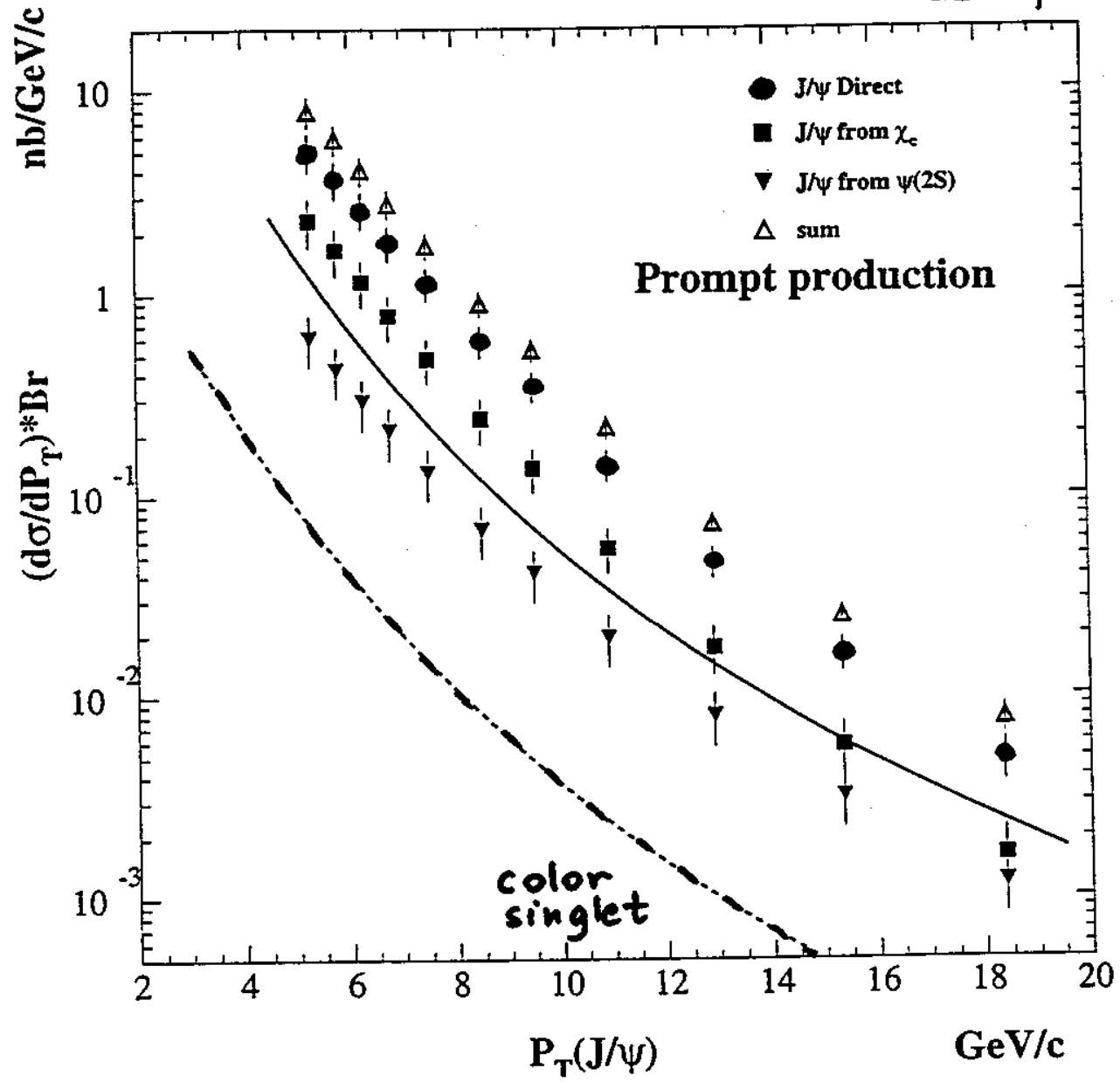
$$F(N_o b)_\chi^\psi = F_\chi^\psi \cdot \frac{1 - F_b^\chi}{1 - F_b^\psi} = F_\chi^\psi \cdot (1.085 \pm 0.04)$$

CDF XXXXXXXXXX PRL 79



Fraction vs p<sub>T</sub><sup>ψ</sup>

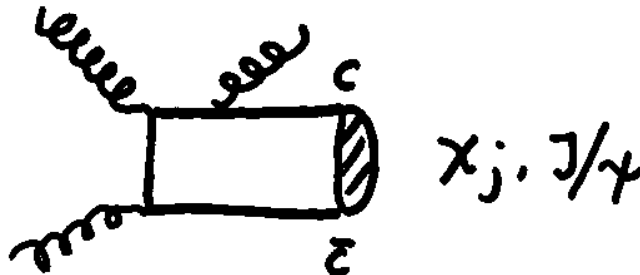
$p_T^\psi > 4.0$	$0.32 \pm 0.02 \pm 0.09$
$4.0 < p_T^\psi < 6.0$	$0.33 \pm 0.03 \pm 0.09$
$6.0 < p_T^\psi < 8.0$	$0.31 \pm 0.03 \pm 0.08$
$8.0 < p_T^\psi < 10.0$	$0.26 \pm 0.04 \pm 0.07$
$p_T^\psi > 10.0$	$0.27 \pm 0.05 \pm 0.08$



## Charmonium production Models

- **Color Evaporation (local-duality)**

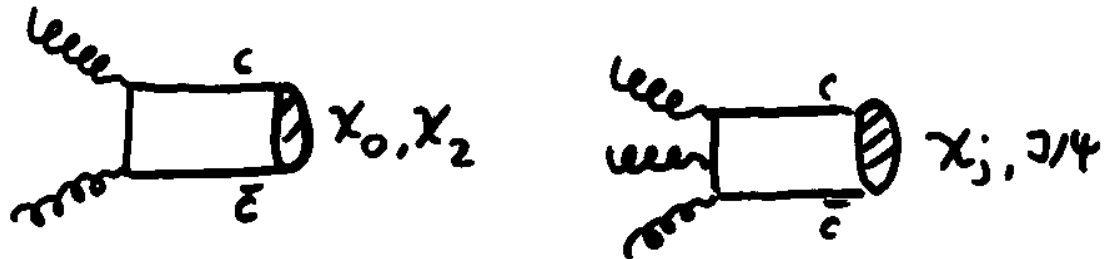
H. Fritzsch PL 67B, 217(1977), R. Gavai *et al.* LJ of MP A10, 3043(1995),  
 J. Amundson *et al.* PL B390, 323 (1997).



directly produced charmonium meson is not constrained to the same  $J^{PC}$  state as the  $c\bar{c}$  pair produced in the hard scatter

- **Color Singlet Model**

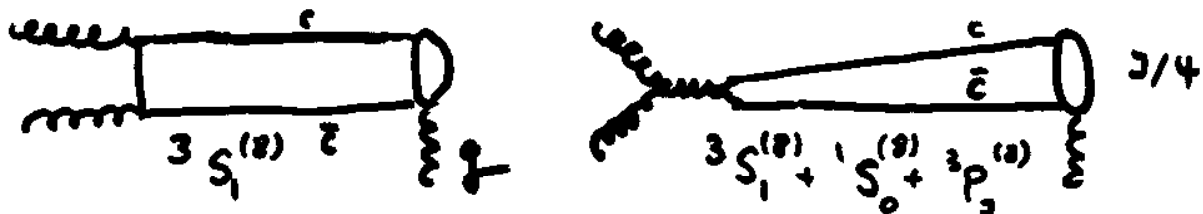
R. Baier, R. Ruckl, ZP C19, 251(1983),  
 M. Vaaninen *et al.* PR D51, 3332(1995); G. Schuler CERN-TH.7170/94.



charmonium meson retains the quantum numbers of the  $c\bar{c}$  pair

- **Color Octet Model**

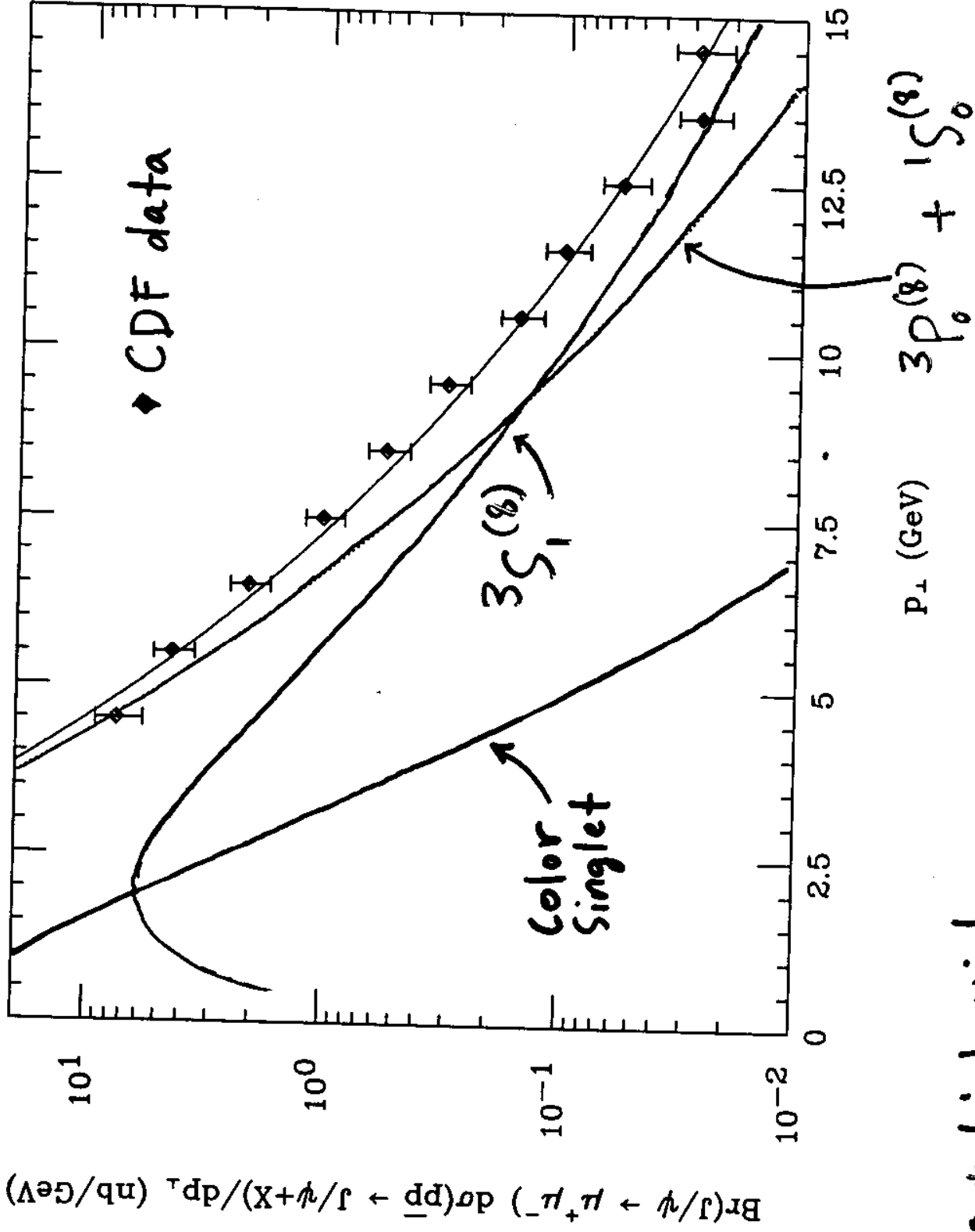
E. Braaten and S. Fleming PRL 74, 3327 (1995); P. Cho, A. Leibovitch PR D53  
 150(1996); 6203(1996)



takes into account the production of  $c\bar{c}$  pairs in a color-octet configuration as  $c\bar{c}$  pair emits a long wavelength gluon far away from the collision point

# Direct $J/\psi$

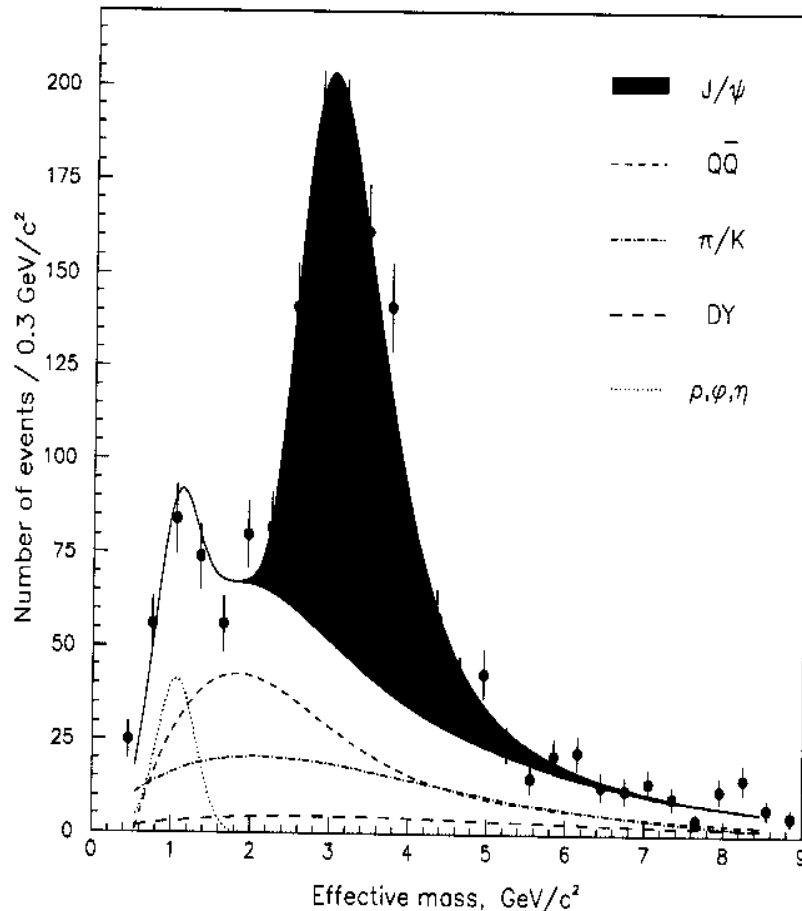
$\chi$ 's removed  
 $b$ 's removed



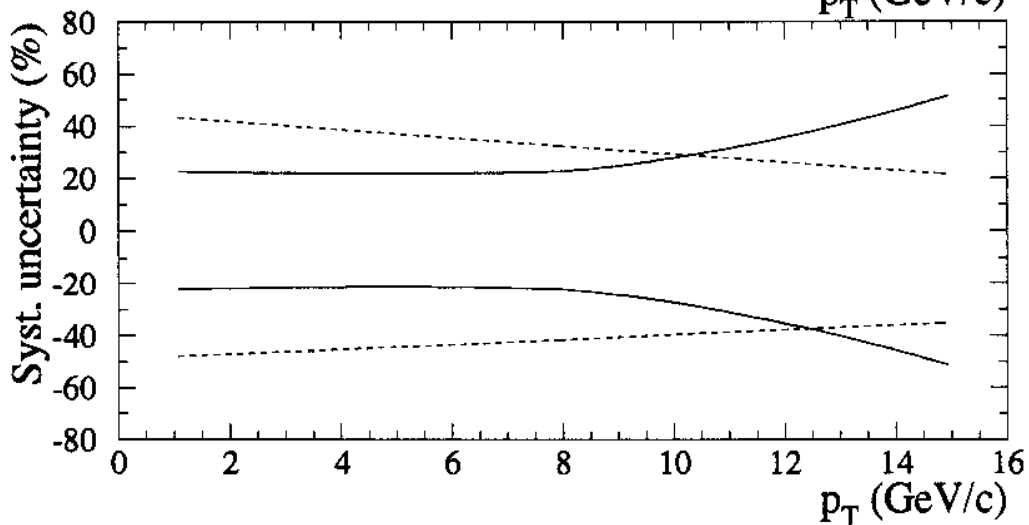
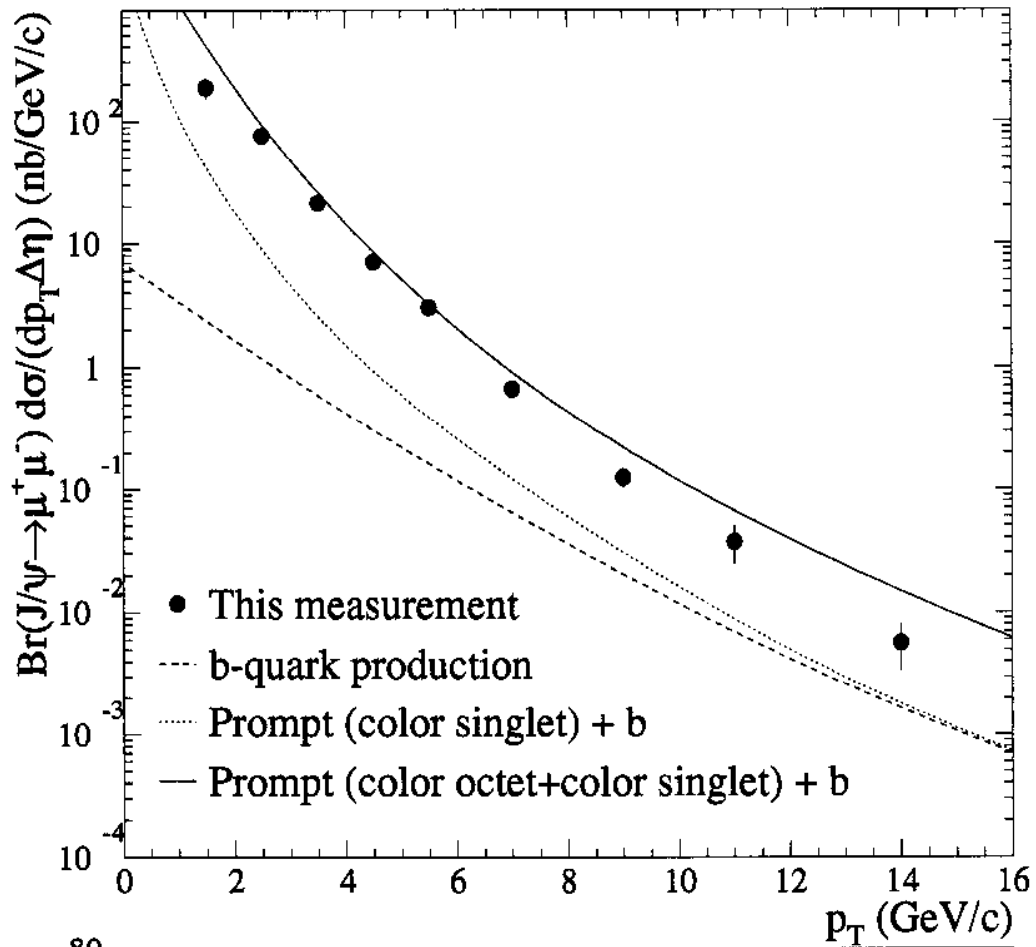
Cho + Liebovich  
PRD 53 6203 (1996)

## Inclusive Forward $J/\psi$ Production (DØ)

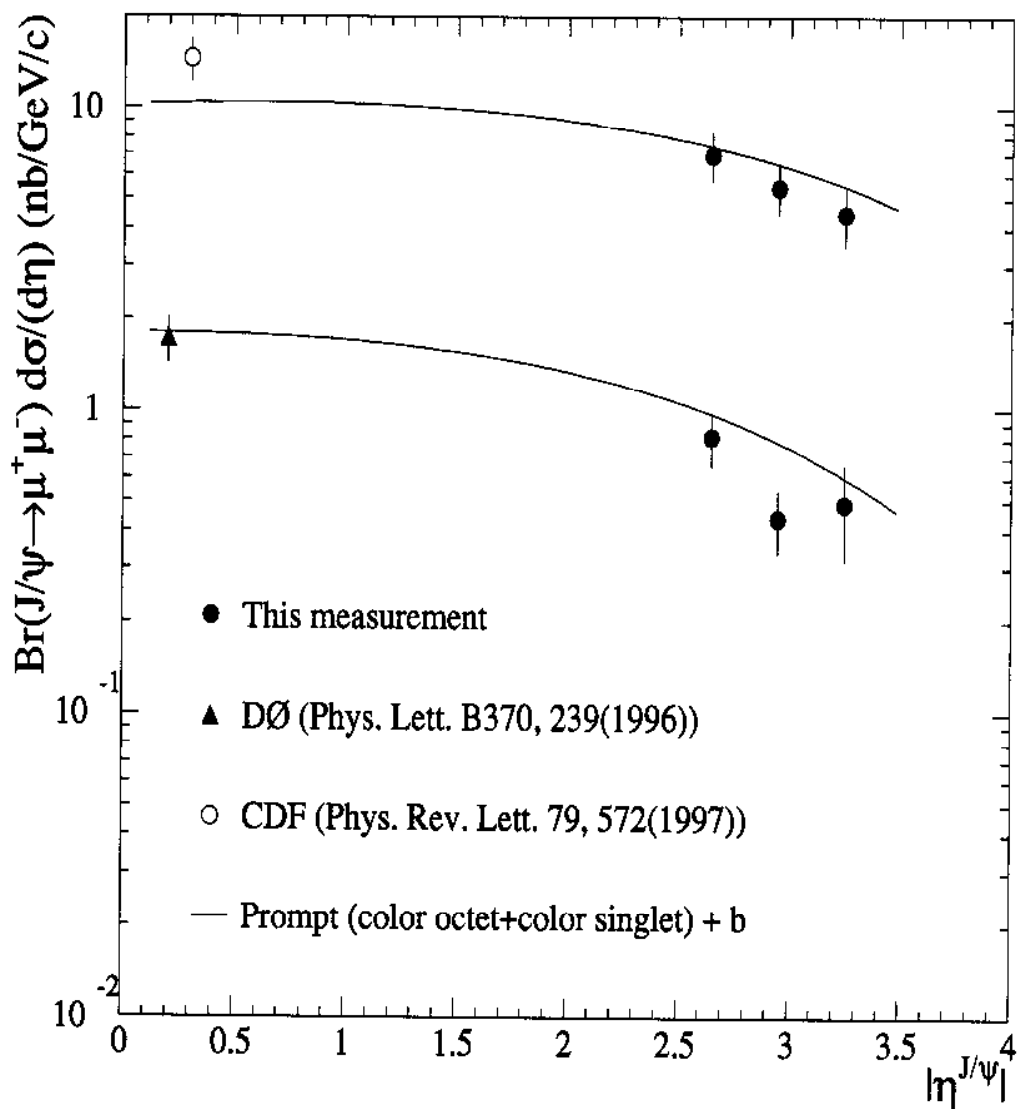
- Analysis based on Small Angle Muon System (SAMUS)
- 1994-95 data (prescaled di $\mu$  triggs) -  $\int \mathcal{L} dt = 9.8 \pm 0.5 \text{ pb}^{-1}$
- Data selection:
  - Level1 hit multiplicity cut ( $\epsilon$  from the data)
  - Single interaction events
  - $2.4 < |\eta^\mu| < 3.2$
  - leading  $\mu$  with  $p_T^\mu > 3 \text{ GeV}/c$ ;  $p^\mu < 150 \text{ GeV}/c$
  - Quality cuts;  $>14$  hits/track (max: 18)
- $\Rightarrow 1779 \mu^+ \mu^-$  ;  $281 \mu^\pm \mu^\pm$  events
- Fitted  $J/\psi$  events:  $740 \pm 80$  ( $2.5 < |\eta^{J/\psi}| < 3.7$ )



## $p_T$ Dependence of Forward $J/\psi$ Production



# Rapidity Dependence of Forward $J/\psi$ Production



- Color octet model predictions agree with the data.

## Conclusions (ONIA Production)

- CDF published results on the central ( $|\eta^{J/\psi}| < 0.6$ )  $J/\psi$  and  $\psi(2s)$  production:
  - fraction of  $J/\psi$  and  $\psi(2s)$  originating from  $b$  hadrons increases with  $p_T$  from 15% ( $p_T(J/\psi) = 5 \text{ GeV}/c$ ) to 40% ( $p_T(J/\psi) = 18 \text{ GeV}/c$ )
  - $B \rightarrow J/\psi + X$  production consistent with other CDF and DØ  $B$  cross section results
  - fraction of  $J/\psi$  originating from  $\chi_c$  decays is  $29.7 \pm 1.7 \pm 5.7 \%$  ( $p_T(J/\psi) > 4 \text{ GeV}/c$ )
  - DØ cross section,  $f_b$  and  $f_\chi$  measurements are consistent with the CDF results.
  - direct  $J/\psi$  and  $\psi(2s)$  productions are in excess of the predictions of the Color Singlet Model by a factor  $\approx 50$
  - Color Octet Model can fit the CDF data
- Rapidity Dependence of  $J/\psi$  Production (DØ)
  - color octet model, with matrix elements fitted to the CDF data for the central  $J/\psi$  production, describes the data in the  $(2.5 < |\eta^{J/\psi}| < 3.7)$  range.
- Work in Progress
  - $J/\psi$  and  $\psi(2s)$  polarization measurements (CDF)



## Conclusions (B Production)

- Measured *b* cross section at  $|y_b| < 1$  exceeds NLO QCD predictions by  $\times 2.5 - 3$ .
- Measured (preliminary) *b* cross section at  $|y_b| \approx 3$  is  $\approx 3 - 4$  times higher than NLO QCD prediction (DØ)
- Measured (preliminary)  $b\bar{b}$  cross section at ( $|\eta_{b1}| < 1.5, 1.8 < |\eta_{b2}| < 2.6$ ) is  $\approx 2.4$  times higher than NLO QCD prediction (CDF).
- CDF measurement of central-forward to central-central cross section ratio:

$$R_{\text{data}} = 0.361 \pm 0.041(\text{stat})_{-0.023}^{+0.011}(\text{syst})$$

in agreement with NLO QCD prediction:

$$R_{\text{theory}} = 0.338_{-0.097}^{+0.014}$$

- Result sensitive to gluon distribution in the proton for  $x > 0.15$  but higher statistics needed to distinguish between various parton distribution sets.