

Hyperon physics - the future?

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~ what I would like to do next...

$\Sigma^\pm$ semileptonic decays

* Why are they interesting?

→ to measure purity of Λ

(is there a small mixing with Σ^0 ?)

u-d quark mass difference breaks isospin symmetry of strong interaction,

So the mass eigenstates are

$$\Lambda = \Lambda_8 \cos \phi + \Sigma_8^0 \sin \phi$$

$$\Sigma^0 = -\Lambda_8 \sin \phi + \Sigma_8^0 \cos \phi$$

How big is the mixing angle ϕ ?

$$\begin{array}{ccc} \Sigma^+ & \xrightarrow{6.9 \text{ MeV}} & \Sigma^0 & \xrightarrow{3.2 \text{ MeV}} & \Sigma^- \\ & & \downarrow 77 \text{ MeV} & & \\ & & \Lambda & & \end{array}$$

Σ^0 lies about 0.9 MeV above the mid point

$$M_{\Sigma^0} - M_{\Lambda} = 77 \text{ MeV}$$

$$\text{Notice } \frac{0.9}{77} = 1.2\%$$

Kaul (Phys Lett B 328, 149 (1994))

& Henley & Miller (HEP-PA-9408227)

estimate $\phi \approx 1.3\% - 1.5\%$

② * How to observe this?

perhaps by $\Sigma^0 \rightarrow \Lambda \gamma$ transition? (E-M)

$\mu(\Sigma\Lambda)$ measured by Primakoff effect = -1.61 ± 0.08 nm

Theory (simple quark model):

$$\mu(\Sigma\Lambda) = \frac{1}{\sqrt{3}} (\mu_d - \mu_u) = -1.63 \text{ nm}$$

so this measurement is inconclusive.

Related transitions: $\Sigma^\pm \rightarrow \Lambda e^\pm \nu$

now with a small piece of $\Sigma^\pm \rightarrow \Sigma^\pm_8 e^\pm \nu$ added,
which will change the situation.

$$\Sigma^+ \quad \Sigma^- = s \underline{u} \underline{u} \quad s \underline{d} \underline{d} \quad u \underline{u}, d \underline{d} = \text{spin } 1$$

$$\Sigma^\pm_8 = s \underline{u} \underline{d} \quad u \underline{d} = \text{spin } 1$$

$$\Lambda_8 = s \underline{u} \underline{d} \quad \underline{u} \underline{d} = \text{spin } 0$$

in these decays, s quark is a spectator

$\Sigma^- \rightarrow \Sigma^\pm_8$ (spin 1 - spin 1) can be a Fermi transition f_1
or Gamow-Teller g_1

Cabibbo theory: $f_1 = \sqrt{2} \quad g_1 = \sqrt{2} F$

$\Sigma^- \rightarrow \Lambda_8$ (spin 1 - spin 0) can only be G-T

Cabibbo theory: $f_1 = 0 \quad g_1 = \sqrt{\frac{2}{3}} D$

(Cabibbo theory has 3 parameters, $F, D, \sin \theta_c$)

③ Now if $\Lambda = \Lambda_8 \cos \phi + \Sigma_8^0 \sin \phi$

$$f_1: 0 \rightarrow \sqrt{2} \sin \phi$$

$$g_1: \sqrt{\frac{2}{3}} D \rightarrow \sqrt{\frac{2}{3}} D \cos \phi + \sqrt{2} F \sin \phi$$

Observables Decay rate $\propto (f_1^2 + 3g_1^2)$

$$\frac{2}{3} D^2 \rightarrow \frac{2}{3} D^2 + \frac{4}{\sqrt{3}} DF \phi$$

$$\text{i.e. } \Gamma(\Sigma^- \rightarrow \Lambda e^- \nu) = \Gamma_0 \left(1 + \frac{2\sqrt{3} F}{D} \phi\right)$$

since $\frac{F}{D}$ is experimentally ≈ 0.63 , the correction becomes $\approx +3\%$

and for $\Sigma^+ \rightarrow \Lambda e^+ \nu$ it is -3%

ie a difference of $\sim 6\%$ due to the mixing.

NB A larger, but easily calculable difference is the ratio of phase space in the two decays, because of the difference of $\Sigma^\pm$ mass:

$$R = \frac{\Gamma_+}{\Gamma_-} = \left(\frac{M_{\Sigma^+} - M_\Lambda}{M_{\Sigma^-} - M_\Lambda} \right)^5 \left(1 + 3 \frac{M_{\Sigma^-} - M_{\Sigma^+}}{M_{\Sigma^-} - M_\Lambda} \right)$$

0.59 0.61

one might also hope to measure f_1/g_1 in each decay:

This = 0 without mixing and $\rightarrow \mp \frac{\sqrt{3}}{D} \phi$ with mixing

$$= \mp 0.03$$

Measure Λ spin direction (by $\Lambda \rightarrow p \pi^-$)
asymmetry to e, ν direction

④

* What has been done already?

$$\tau_{\Sigma^-} = 1.48 \times 10^{-10} \text{ s} \quad \text{BR}(\Sigma^- \rightarrow \Lambda e^- \nu) = (5.73 \pm 0.25) \times 10^{-5}$$

(1843 events would total: 1620 events WA2)

$$\rightarrow \Gamma_- = \frac{5.7 \times 10^{-5}}{1.48 \times 10^{-10}} = 3.87 \times 10^5 \text{ s}^{-1} \quad (\pm 5\%)$$

$$\tau_{\Sigma^+} = 0.8 \times 10^{-10} \text{ s} \quad \text{BR}(\Sigma^+ \rightarrow \Lambda e^+ \nu) = (2.0 \pm 0.5) \times 10^{-5}$$

(21 events would total)

$$\rightarrow \Gamma_+ = \frac{2 \times 10^{-5}}{0.8 \times 10^{-10}} = 2.5 \times 10^5 \text{ s}^{-1} \quad (\pm 25\%)$$

$$\text{So } \frac{\Gamma_+}{\Gamma_-} = \frac{2.5}{3.87} = 0.65 \pm 0.17 \quad (\text{cf } 0.61)$$

inconclusive!

Can we improve on this?

→ Measure $\frac{\Gamma_+}{\Gamma_-}$ to better than 1%?

So need to measure $\gg 10,000$

of each decay $\Sigma^+ \rightarrow \Lambda e^+ \nu$
 $\Sigma^- \rightarrow \Lambda e^- \nu$

⑤

10,000 s.l. decays means $\frac{10^4}{5.7 \times 10^{-5}} = 1.75 \times 10^8 \quad \Sigma^-$

and $\frac{10^4}{2 \times 10^{-5}} = 5 \times 10^8 \quad \Sigma^+$

Typical beam fractions at 330 GeV/c: $\Sigma^- \sim 30\%$ (foreground π^-)
 $\Sigma^+ \sim 1\%$ (foreground p/π^+)

If beam rate = 10^7 s^{-1}

Trigger live time = 10% (??)

SPS duty cycle = $\frac{2.2}{14.5} = 15\%$

SPS efficiency = 70%

} 1%

We will have $3 \times 10^4 \text{ s}^{-1}$ of Σ^-

or 10^3 s^{-1} of Σ^+

} in real time

of these, perhaps 30% of Σ^- decay in fiducial volume of length 5m

$\lambda_{\Sigma^-} = 12.2 \text{ m}$ at 330 GeV/c

and 50% of Σ^+ decay $\lambda_{\Sigma^+} = \text{~~12.2~~ } 6.65 \text{ m}$

If experiment acceptance $\approx 50\%$ (??) see later...

Then running time $\Sigma^- = \frac{2 \times 10^8}{0.5 \times 0.3 \times 3 \times 10^4} = 4 \times 10^4 \text{ s}$
 $\boxed{= 12 \text{ hr}}$

& running time $\Sigma^+ = \frac{5 \times 10^8}{0.5 \times 0.5 \times 10^3} = 2 \times 10^6 \text{ s}$
 $\boxed{= 3-4 \text{ weeks}}$

②
* Trigger

e^+ - TRD / Lead glass

Λ - multiplicity

(e threshold?)

($\Lambda \rightarrow p \pi^-$ BR : 64%)

* Backgrounds

$\Xi^- \rightarrow \Lambda \pi^-$ fw -ve beam

$\uparrow$ 1% of Σ^- ?

Inelastic collisions producing Λ and π^0 ($\rightarrow$ em showers)
fw both +ve and -ve beam $\Rightarrow$ helium bags

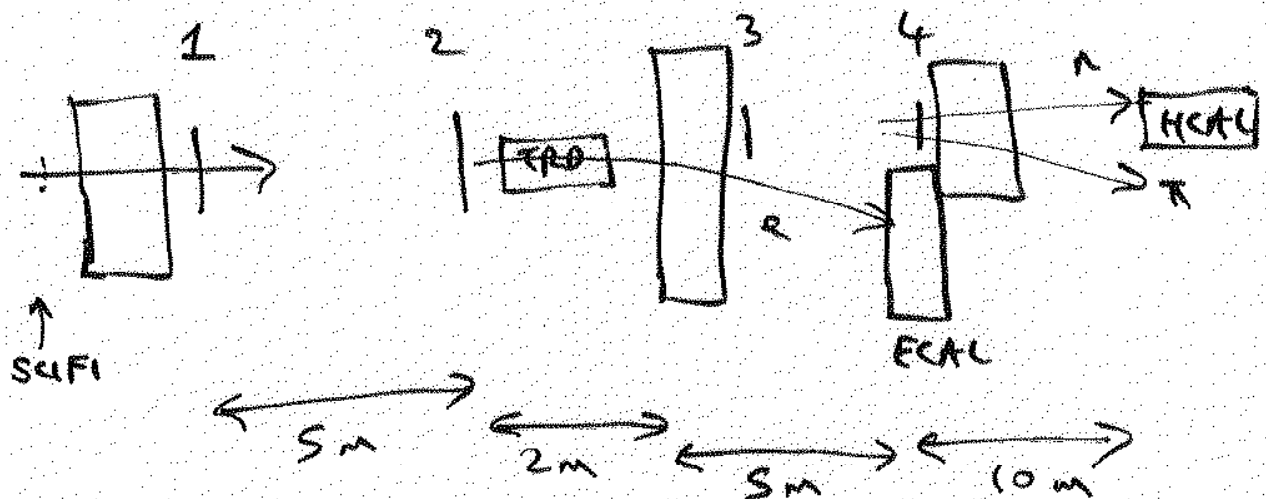
* Normalisation

$\Sigma^- \rightarrow \pi \pi^-$ [NB $\Sigma^+ \rightarrow \pi \pi^+$]

$\Sigma^+ \rightarrow \begin{matrix} p \pi^0 \\ n \pi^+ \end{matrix}$

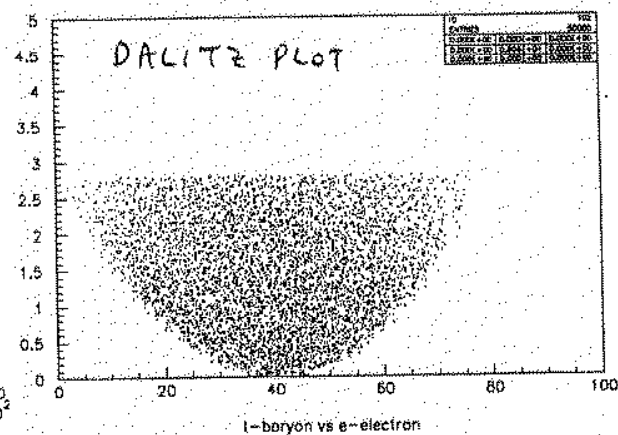
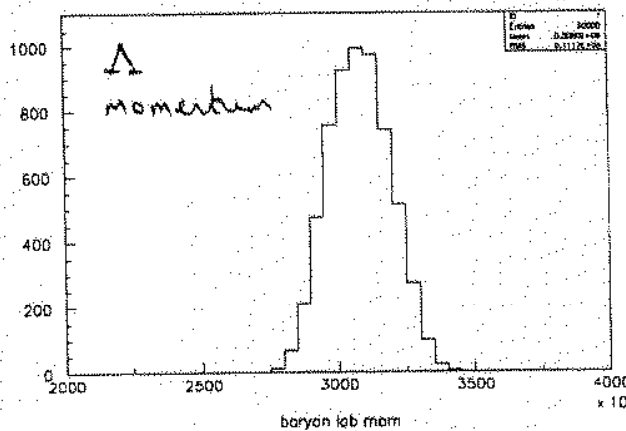
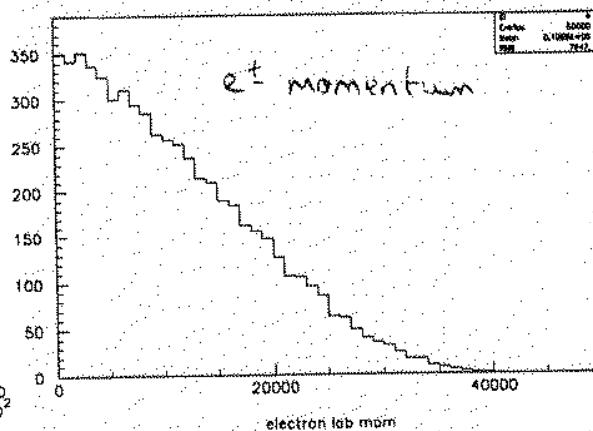
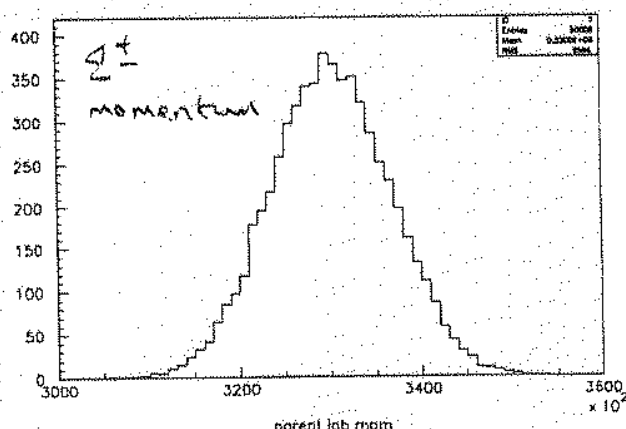
(need hadron calorimeter)

Need good momentum resolution fw incident hyperon
 $\rightarrow$ scifi hodoscope?



$$\Sigma^{\pm} \rightarrow \Lambda e^{\pm} \nu \quad f_1=0 \quad g_1=1$$

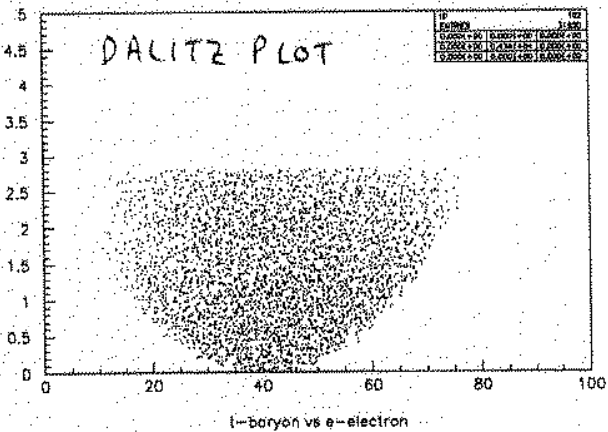
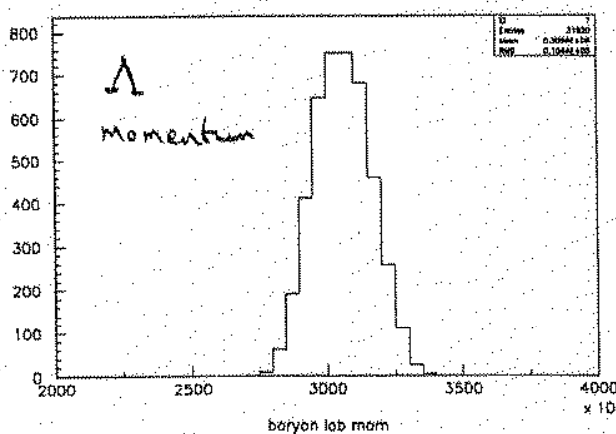
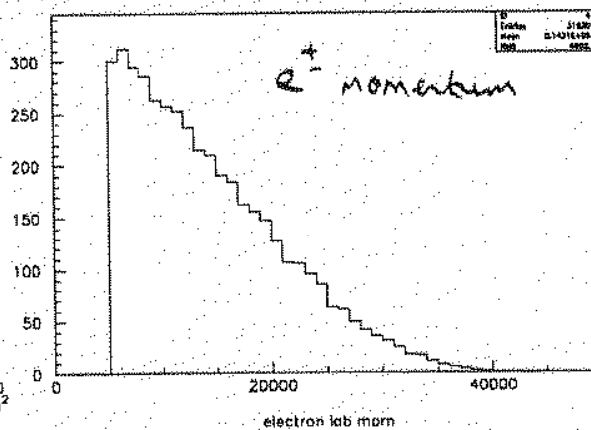
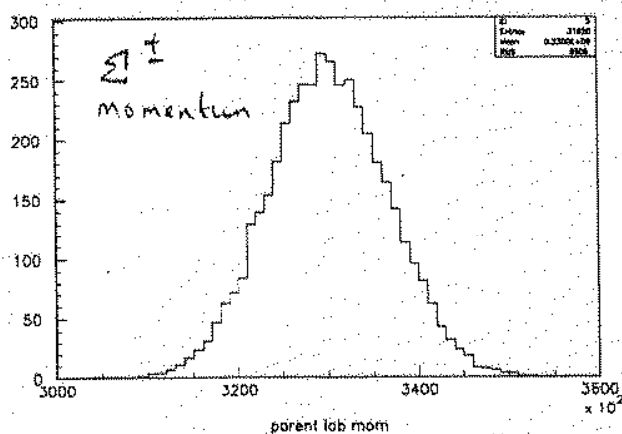
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8)

$$\Sigma^+ \rightarrow \Lambda e^+ \nu \quad f_1=0 \quad g_1=1$$

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[5 GeV cut on electron]