

# Predictive Power!

## STRIKING RESULTS OF SZ66

$$177 \text{ MeV} = M_\Delta - M_N = \frac{3(M_K^* - M_K) + (M_\pi - M_\eta)}{4} = 180 \text{ MeV}$$

$\boxed{\frac{M_\Delta - M_N}{M_{\Sigma^*} - M_\Sigma}} = 1.53$	$\boxed{\frac{M_\rho - M_\pi}{M_{K^*} - M_K}} = 1.61$
<b>Baryons</b>	<b>Mesons</b>

Extension by DGG-HJL et al

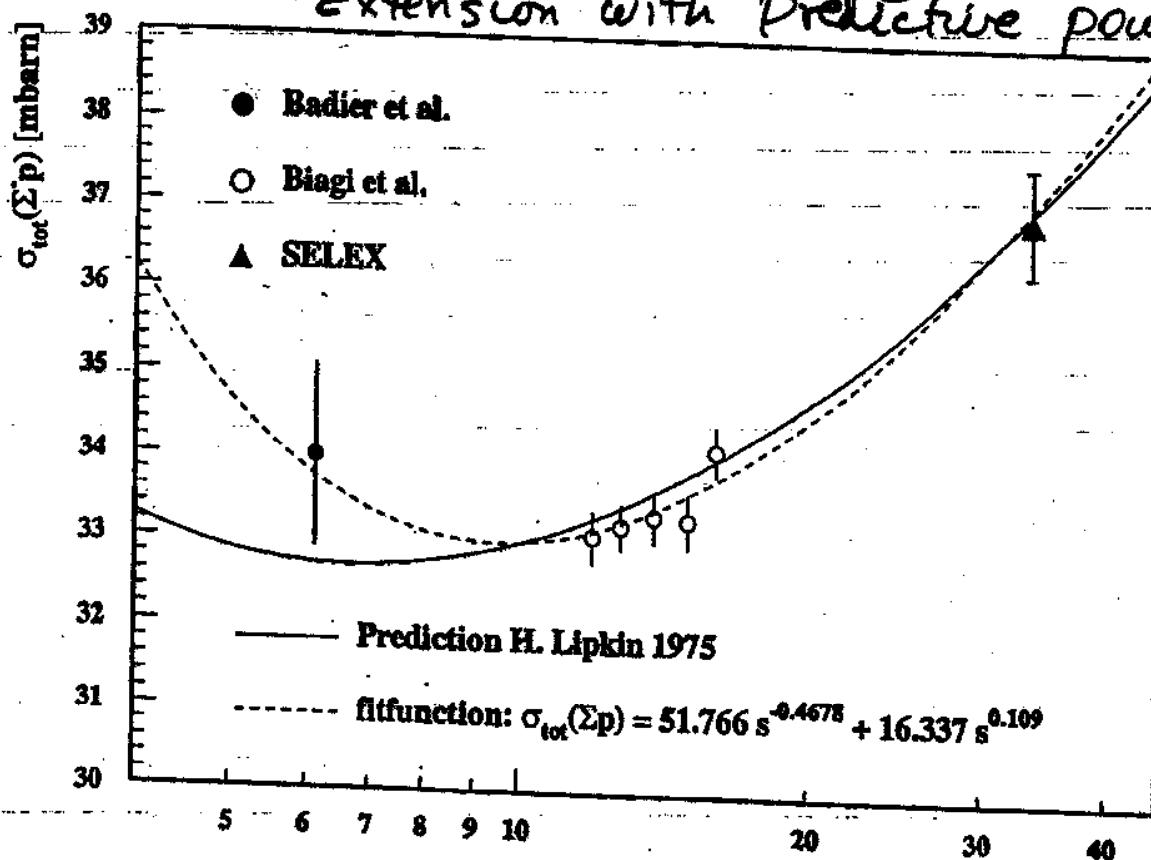
— Hyperfine Interaction —

$$0.88 \text{ n.m.} = \mu_p + \mu_n = \frac{2 M_p}{M_N + M_\Delta} = 0.865$$

$$-0.61 \text{ n.m.} = \mu_\Delta = -\frac{\mu_p}{3} \cdot \boxed{\frac{M_{\Sigma^*} - M_\Sigma}{M_\Delta - M_N}} = -0.61$$

Levin-Frankfurt  $\sigma_{\text{tot}}(\text{pp}) \approx \frac{2}{3} \sigma_{\text{tot}}(\text{p}p)$

Extension with Predictive power



# Hyperon Decays and $SU(3)$

"Where is the physics? Not in  $D \& F$ "

## Bjorken Sum Rule

$$\frac{G_A}{G_V} (n \rightarrow p) = (\Delta u - \Delta d)_p = (\Delta d - \Delta s)_n$$

$SU(3)$  then gives

$$\begin{aligned} \frac{G_A}{G_V} (\Sigma^- \rightarrow n) &= (\Delta s - \Delta u)_{\Sigma^-} = (\Delta d - \Delta s)_p \\ &= \frac{1}{2} [(\Delta s - \Delta u)_{\Sigma^-} + (\Delta u - \Delta s)_n] \end{aligned}$$

New  
Data!

$$\boxed{\frac{G_A}{G_V} (\Xi^0 \rightarrow \Sigma^+) = (\Delta s - \Delta u)_{\Xi^0} = (\Delta u - \Delta d)_p}$$

How is  $SU(3)$  broken?

Weak and Strong  $SU(3)$ .

Weak  $SU(3)$  OK

Current algebra. Cabibbo Theory  
CKM Matrix. Current Algebra Sum Rule

Strong  $SU(3)$  broken  $m_s > m_u, m_d$

$$M_K \gg M_\pi$$

$$(\Delta s - \Delta u)_{\Sigma^-} \neq (\Delta u - \Delta s)_n$$

# New Interesting result

$$\frac{G_A}{G_V}(\Xi^* \rightarrow \Sigma^+) = \frac{G_A}{G_V}(n \rightarrow p)$$

SU(3) says this means that

$$(\Delta s - \Delta u)_{\Xi^*} = (\Delta u - \Delta d)_p$$

If strange sea is suppressed this is clearly wrong!

But Current Algebra says that

$$[\delta(\Delta s - \Delta u)_{\Xi^*} + (\Delta u - \Delta s)_{\Xi^*}] = \frac{1}{2}[(\Delta u - \Delta d)_p + (\Delta d - \Delta u)_p]$$

This is immune to strange Sea Suppression in all baryons

# Predictions and Experimental Values of $G_A/G_V$

<i>Decay</i>	<i>SU</i>	<i>Constit.</i>	<i>SU(3)</i>	<i>Experiment</i>
	(6)	<i>SU(6)</i>		

$n \rightarrow p$	$\frac{5}{3}$	<i>input</i>	<i>input</i>	$1.261 \pm .004$
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$\Lambda \rightarrow p$	1	0.756	$0.727 \pm .007$	$0.718 \pm .015$
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$\Xi^- \rightarrow \Lambda$	$\frac{1}{3}$	0.252	$0.193 \pm .012$	$0.25 \pm .05$
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$\Sigma^- \rightarrow n$	$-\frac{1}{3}$	-0.252	<i>input</i>	$-0.340 \pm .017$
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$\frac{\Sigma^- \rightarrow n}{\Lambda \rightarrow p}$	$-\frac{1}{3}$	$-\frac{1}{3}$	<i>none</i>	$-0.473 \pm .026$
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*SU(3) equal spacing rule*

$$\frac{\left(\frac{g_\mu}{g_\nu}\right)_{\Lambda \rightarrow p}}{\left(\frac{g_\mu}{g_\nu}\right)_{\Sigma^- \rightarrow n}} \cdot \frac{\mu_{\Sigma^+} + 2\mu_{\Sigma^-}}{3\mu_\Lambda} = 0.12 \pm 0.04$$

$$\Delta s(\Lambda)_{SU(3)} = 1$$

$$\Delta s(\Sigma)_{SU(3)} = -1/3$$

$$\frac{\Delta s(\Sigma)_{SU(3)}}{\Delta s(\Lambda)_{SU(3)}} = \frac{\left(\frac{g_\mu}{g_\nu}\right)_{\Sigma^- \rightarrow n}}{\left(\frac{g_\mu}{g_\nu}\right)_{\Lambda \rightarrow p}} = \frac{\mu_{\Sigma^+} + 2\mu_{\Sigma^-}}{3\mu_\Lambda} = -1/3$$

whereas experimentally

$$\frac{\left(\frac{g_\mu}{g_\nu}\right)_{\Sigma^- \rightarrow n}}{\left(\frac{g_\mu}{g_\nu}\right)_{\Lambda \rightarrow p}} = -0.473 \pm 0.026$$

$$\frac{\mu_{\Sigma^+} + 2\mu_{\Sigma^-}}{3\mu_\Lambda} = -0.03 \pm 0.02$$

**SU(3) symmetry gives the relations:**

$$\Delta u(p) = \Delta d(n) = \Delta u(\Sigma^+) = \Delta d(\Sigma^-) = \Delta s(\Xi^0) = \Delta s(\Xi^-)$$

$$\Delta d(p) = \Delta u(n) = \Delta s(\Sigma^+) = \Delta s(\Sigma^-) = \Delta s(\Sigma^0) = \Delta u(\Xi^0) = \Delta d(\Xi^-)$$

$$\Delta s(p) = \Delta s(n) = \Delta d(\Sigma^+) = \Delta u(\Sigma^-) = \Delta d(\Xi^0) = \Delta u(\Xi^-)$$

$$\Delta u(\Sigma^0) = \Delta d(\Sigma^0) = (1/2) \cdot [\Delta u(\Sigma^+) + \Delta d(\Sigma^+)]$$

$$\Delta q(\Sigma^0) + \Delta q(\Lambda) = (2/3) \cdot [\Delta u(n) + \Delta d(n) + \Delta s(n)]$$

These relations allow all the baryon spin structures to be obtained from values of  $\Delta u(n)$ ,  $\Delta d(n)$  and  $\Delta s(n)$

### Baryon Spin Structures

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#### From Nucleon Data and SU(3) Symmetry

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Baryon	$\Delta u$	$\Delta d$	$\Delta s$
$p$	$0.83 \pm 0.03$	$-0.43 \pm 0.03$	$-0.10 \pm 0.03$
$n$	$-0.43 \pm 0.03$	$0.83 \pm 0.03$	$-0.10 \pm 0.03$
$\Sigma^+$	$0.83 \pm 0.03$	$-0.10 \pm 0.03$	$-0.43 \pm 0.03$
$\Sigma^-$	$-0.10 \pm 0.03$	$0.83 \pm 0.03$	$-0.43 \pm 0.03$
$\Xi^0$	$-0.43 \pm 0.03$	$-0.10 \pm 0.03$	$0.83 \pm 0.03$
$\Xi^-$	$-0.10 \pm 0.03$	$-0.43 \pm 0.03$	$0.83 \pm 0.03$
$\Sigma^0$	$0.365 \pm 0.03$	$0.365 \pm 0.03$	$-0.43 \pm 0.03$
$\Lambda$	$-0.165 \pm 0.03$	$-0.165 \pm 0.03$	$0.63 \pm 0.03$

$$\frac{W(q \uparrow \rightarrow B \uparrow)}{W(q \uparrow \rightarrow B \downarrow)} = \frac{q \uparrow(B \uparrow)}{q \uparrow(B \downarrow)} = \frac{q \uparrow(B \uparrow)}{q \downarrow(B \uparrow)}$$

$$P(q \uparrow \rightarrow B) = \frac{W(q \uparrow \rightarrow B \uparrow) - W(q \uparrow \rightarrow B \downarrow)}{W(q \uparrow \rightarrow B \uparrow) + W(q \uparrow \rightarrow B \downarrow)} = \frac{q \uparrow(B \uparrow) - q \downarrow(B \uparrow)}{q \uparrow(B) + q \downarrow(B)}$$

$$P(q \uparrow \rightarrow B) = \frac{\Delta q(B)}{q \uparrow(B) + q \downarrow(B)}$$

Distribution	all quarks	valence quarks
$\Delta u_p$	$0.88 \pm 0.03$	$0.93 \pm 0.03$
$\Delta d_p$	$-0.38 \pm 0.03$	$-0.33 \pm 0.03$
$\Delta s_p$	$-0.05 \pm 0.03$	$0.0 \pm 0.03$
$\Delta u_\Lambda$	$-0.115 \pm 0.03$	$-0.065 \pm 0.04$
$\Delta d_\Lambda$	$-0.115 \pm 0.03$	$-0.065 \pm 0.04$
$\Delta s_\Lambda$	$0.68 \pm 0.03$	$0.73 \pm 0.04$
$\Delta u_{\Sigma^0}$	$0.415 \pm 0.03$	$0.465 \pm 0.04$
$\Delta d_{\Sigma^0}$	$0.415 \pm 0.03$	$0.465 \pm 0.04$
$\Delta s_{\Sigma^0}$	$-0.38 \pm 0.03$	$-0.33 \pm 0.04$
$\Delta u_{\Sigma^-}$		$0.23 \pm 0.02$
$\Delta d_{\Sigma^-}$		$0.23 \pm 0.02$
$\Delta s_{\Sigma^-}$		$0.33 \pm 0.04$